MEASURING CONDITIONS AND UNCERTAINTIES FOR THE COMPARISON AND CALIBRATION OF NATIONAL DOSIMETRIC STANDARDS AT THE BIPM*

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Abstract. Information is presented on the experimental conditions used in the x- and ⁶⁰Co gamma-radiation beams at the BIPM, in the ¹³⁷Cs gamma-radiation beam at the IAEA laboratories and in the MV-radiation beams at the DOSEO platform, for comparisons of national primary standards and calibrations of national secondary standards in terms of air kerma and absorbed dose to water, together with the uncertainties involved in the determination of these dosimetric quantities.

I. Introduction

For each signatory of the Metre Convention and for a given type of measurement, the BIPM works with the National Metrology Institute (NMI) or a laboratory designated nationally for the purpose. For those laboratories that hold national primary standards, the BIPM compares these standards against the BIPM reference standards, either directly using the primary standards in the BIPM reference beams or indirectly through the calibration of transfer instruments by both the BIPM and the NMI. For those that do not hold primary standards, the BIPM calibrates secondary standards that are then normally used as national reference instruments. For this reason, the chambers should be instruments of good quality; in particular with respect to leakage current and both short- and long-term stability.

Comparisons, characterizations and calibrations of ionization chambers are performed by the BIPM in terms of:

- air kerma in the low- (including mammography) and medium-energy x-ray ranges, in ${}^{60}Co$ gamma radiation (at the BIPM), and in $137Cs$ gamma radiation (at the IAEA laboratories);
- absorbed dose to water in medium-energy x-ray beams, in ⁶⁰Co gamma radiation (at the BIPM), and in MVradiation beams (at the DOSEO platform).

The present report documents the BIPM measurement conditions, the values for the physical constants and correction factors, and the estimated uncertainties in the determination of the primary quantities and of calibration coefficients.

II. General remarks

The reference plane is specified in terms of a distance from the radiation source or, in the case of low-energy x-rays, from the beam exit window. The reference point is the intersection of the beam axis with the reference plane.

For chamber types other than parallel plate, the chamber is positioned with its axis in the reference plane and with the stated point of measurement of the chamber at the reference point. For measurements in air in gamma radiation the chamber is used with the build-up cap provided. The orientation of the chamber is such that the number, text or line inscribed on the stem faces the radiation source, unless a different orientation is indicated. Parallel-plate chambers are calibrated with the front surface of the chamber casing in the reference plane, unless a different surface is indicated on the chamber, and with the entrance window centred on the beam axis.

All chambers are irradiated for at least thirty minutes, with the appropriate polarizing potential applied to the outer electrode (wall or window), before any measurements are made. If the NMI applies a potential of a given polarity to the collecting electrode, the BIPM will apply the same potential with opposite polarity to the outer electrode to create an equivalent electric field within the air cavity.

The leakage current is normally measured before and after each set of measurements and a correction applied based on the mean value. A chamber for which the relative leakage current is high, and in particular for which the leakage is also variable, is unsuitable for use as a transfer instrument and might also be considered unsuitable for calibration. In the latter case, a study note is issued.

The irradiation facilities at the BIPM and at the IAEA laboratories are temperature controlled (close to 20 °C) at the level of around 100 mK. For air-kerma measurements in ${}^{60}Co$, an additional, passive enclosure is used to ensure temperature stability below 0.1 °C. At the DOSEO platform the air temperature is controlled in the range from 20 °C to 24 °C and air temperature variations over an instrument calibration are typically 0.5 °C. For absorbed-dose measurements in water at the BIPM and at the DOSEO platform the water temperature variations over an instrument calibration are typically 0.2 °C. The BIPM reference conditions for temperature, pressure and relative humidity are $T_0 = 293.15$ K, $P_0 = 101.325$ kPa and 50 %, respectively. As the relative humidity is controlled within the range 40 % to 55 %, no humidity correction is applied.

Calibration of national standards: No correction is applied for lack of saturation for x-ray, ¹³⁷Cs and ⁶⁰Co radiation beams; the air-kerma rate or absorbed-dose-to-water rate is stated in the certificate. For the thimble chamber types calibrated in gamma radiation and in air-kerma for medium-energy x-rays, the radial nonuniformity correction for the BIPM beams is small and is stated in the certificate, although no correction factor is applied. For the waterproof thimble chamber types calibrated in terms of absorbed dose to water in mediumenergy x-rays, the correction factor at the reference depth will be similar at both laboratories and again no correction factor is applied. In low-energy x-rays, chambers of larger dimensions may be calibrated and the radial uniformity of the beam shows more variation from one laboratory to another. For these reasons, the appropriate correction factor is always applied. Corrections for lack of saturation and for the radial nonuniformity of the beam are applied for calibrations in MV-radiation beams and stated in the certificate.

Comparisons of national standards: The treatment of correction factors depends to some extent on the practice at the NMI and no general statement can be made; the measuring conditions adopted are clearly stated in the comparison report.

Details of the BIPM conditions of measurement and the uncertainties in the determination of the rates of air kerma and absorbed dose to water are given in Tables 1 to 6 for x-rays, in Tables 7 to 9 for 60Co, in Tables 10 to 12 for MV-radiation beams and in Tables 13 and 14 for $137Cs$. In these tables, the relative standard uncertainties estimated by statistical methods (Type A) are denoted by u_{iA} and those estimated by other means (Type B) are denoted by *ui*B*ⁱ* .

III. Comparison and calibration in terms of air kerma (x-rays, 137Cs, 60Co)

The primary standard, transfer chamber or national reference standard is operated in air at the stated reference distance. The ionization current *I* is determined under the BIPM reference conditions of air temperature, pressure and humidity. The value of *I* is given by

$$
I = I_{\exp}\left(\frac{T}{T_0}\right)\left(\frac{P_0}{P}\right) \tag{1}
$$

where I_{exp} is the ionization current measured at temperature *T* (expressed in K) and pressure *P* (expressed in kPa).

For a transfer chamber or national reference standard, the calibration coefficient N_K is defined by the relation

$$
N_K = \dot{K}_{\text{BIPM}} / I,\tag{2}
$$

where ${\dot K}_{\rm BIPM}$ is the air-kerma rate at the reference point, measured with the BIPM standard.

IV. Comparison and calibration in terms of absorbed dose to water (x-rays, 60Co, MV-radiation beams)

⁶⁰Co gamma radiation

When a primary standard is compared directly, the measuring conditions are stated clearly in the comparison report. For indirect comparisons and calibrations, the transfer chamber or national reference standard is placed in its waterproof sleeve (unless calibration of a waterproof chamber without a sleeve is requested) and positioned in the BIPM cubic water phantom of side 30 cm. Its axis is placed in the reference plane, at the reference depth of 5 g cm−² in water. This depth includes the window of the phantom (PMMA, 0.476 g cm−2) and is corrected for the change in water density with temperature. As well as correctly orienting the chamber, a reference mark on the sleeve (if used) is rotated so as to point towards the radiation source, unless a different orientation is indicated.

The calibration coefficient *ND,*^w is determined using the relation

$$
N_{D,w} = \dot{D}_w / (I_w k_{\rm win}),\tag{3}
$$

where:

 \dot{D}_w is the absorbed-dose-to-water rate at the reference point, measured using the BIPM standard at a depth of 5 g cm[−]² in water;

 $I_{\rm w}$ is the ionization current measured using the chamber under the BIPM reference conditions of water temperature, pressure and humidity;

 k_{win} = 0.9997 is a correction factor applied to I_w for the non-equivalence with water of the PMMA window of the phantom (required because a similar factor is applied to the BIPM standard).

Medium-energy x-ray beams

Only waterproof thimble chamber types are accepted and are measured without a waterproof sleeve. For indirect comparisons and calibrations, the transfer chamber or national reference standard is positioned in the BIPM cubic water phantom of side 20 cm. Its axis is placed in the reference plane, at the reference depth of 2 g cm−² in water. This depth includes the window of the phantom (PMMA, 0.200 g cm^{-2}). Because of the shallow depth, no correction is required for the change in water density with temperature.

The calibration coefficient *ND,*^w is determined using the relation

$$
N_{D,w} = \dot{D}_w / I_w,\tag{4}
$$

where:

 \dot{D}_w is the absorbed-dose-to-water rate at the reference point at a depth of 2 g cm⁻² in the water phantom, determined by the BIPM standard;

 $I_{\rm w}$ is the ionization current measured using the chamber under the BIPM reference conditions of water temperature, pressure and humidity.

At the BIPM, the absorbed dose to water is derived from the air-kerma determination.

MV-radiation beams

For indirect comparisons and calibrations, the transfer chamber or national reference standard is placed in its waterproof sleeve (unless calibration of a waterproof chamber without a sleeve is requested) and positioned in the BIPM water phantom of 40 cm x 50 cm x 50 cm. Its axis is placed in the reference plane, at the reference depth of 10 g cm⁻² in water. This depth includes the window of the phantom (PMMA, 0.475 g cm⁻²). As well as correctly orienting the chamber, a reference mark on the sleeve (if used) is rotated so as to point towards the radiation source, unless a different orientation is indicated.

The calibration coefficient *ND,*^w is determined using the relation

$$
N_{D,\mathbf{w}} = \dot{D}_{\mathbf{w}} / (I_{\mathbf{w}} k_s k_{\mathbf{r}}),\tag{5}
$$

where:

 \dot{D}_w is the absorbed-dose-to-water rate at the reference point, measured using the BIPM reference standard at a depth of 10 g cm[−]² in water;

 $I_{\rm w}$ is the ionization current measured using the chamber under the BIPM reference conditions of water temperature, pressure and humidity;

 $k_{\rm s}$ is a correction factor applied to $I_{\rm w}$ for the incomplete collection of charge due to ion recombination, and $k_{\rm rn}$ is a correction factor applied to $I_{\rm w}$ for the radial non-uniformity of the beam.

V. Use of calibration coefficients

A transfer chamber or national reference standard calibrated in the BIPM beam can be used in another beam, taking the calibration coefficients N_K or $N_{D,w}$ to determine *K* or D_w in that beam, subject to certain provisions as listed below:

(a) The humidity conditions must not differ significantly from those of the calibration at the BIPM. If the relative humidity is outside the range 30 % to 70 %, the recommendations of ICRU Report 90 (ICRU 2016) should be used.

(b) The conditions of measurement must not differ significantly from those of the calibration at the BIPM. Otherwise, additional corrections may be necessary as described by Boutillon *et al.* (1993) and Boutillon (1996). Particular attention should be paid to:

- the radiation quality, particularly in the x-ray range;
- the distance from the source;
- the dimensions of the radiation field, in particular with regard to the radiation scattered by the stem and the support for calibration in terms of air kerma;
- the intensity of the ionization current, which can produce a change in the ion recombination;
- the radial non-uniformity of the beam over the cross-section of the chamber.

VI. Comparison and calibration uncertainties

The uncertainties associated with dosimetry measurements made at the BIPM are analysed in accordance with the *Guide to the Expression of Uncertainty in Measurement* (JCGM 2008). The uncertainty budgets for the dosimetry standards are given in Tables 3, 6, 8, 9, 12 and 14. For comparisons, the BIPM standard uncertainties are combined with those associated with the primary or transfer chamber, taking correlation into account, to give the combined standard uncertainty of the comparison results. The detailed uncertainty budgets are given in the comparison report. For the calibration of national reference standards, the BIPM standard uncertainties are combined with the uncertainties associated with the chamber under calibration to give the combined standard uncertainty of the calibration coefficient. This value is given in the calibration certificate.

It is emphasized that the uncertainty associated with BIPM calibrations is a combined *standard* uncertainty without the application of a coverage factor *k*. This long-standing practice of not applying a coverage factor is maintained to facilitate the combination of the BIPM and NMI uncertainties and thus simplify the subsequent dissemination of the standard to the customers of the NMI.

For the purpose of calculating the expanded uncertainty for their end result at a specified level of confidence, an NMI can assume that the effective number of degrees of freedom for a BIPM calibration is sufficient to be able to use a coverage factor *k* = 2 for a level of confidence of approximately 95 %. Any exceptions are noted in the calibration certificate.

Table 1. X-rays (10 kV to 50 kV) Conditions of measurement at the BIPM

 (1) Recommended by Section I of the CCEMRI (1972, 1975).

(2) Mass attenuation coefficient for air.

(3) The more heavily-filtered of the two 50 kV radiation qualities.

 (4) Endorsed by the CCRI (2011).

Table 2. X-rays (10 kV to 50 kV)

Physical constants and correction factors used in the BIPM determination of the air-kerma rate (1)

Dry air density (273.15 K, 101.325 kPa) = 1.2930 kg m⁻³

 $W/e = 33.97$ J C⁻¹

(1) Details on the determination of the air-kerma rate are given in Boutillon *et al.* (1969); correction factors are described by Burns (2004) and Burns *et al.* (2009) for the W-anode qualities and by Kessler *et al.* (2010) for the Mo-anode qualities.

(2) Combined values for k_{ii} and k_{W} adopted from January 2019 (Burns and Kessler 2018).

⁽³⁾ Values at 293.15 K and 101.325 kPa for an attenuation length of 10.0 cm.

⁽²⁾ Combined values for k_{ii} and k_{W} adopted from January 2019 (Burns and Kessler 2018).

(3) Values at 293.15 K and 101.325 kPa for an attenuation length of 10.0 cm.

Table 3. X-rays (10 kV to 50 kV)

Estimated relative standard uncertainties in the BIPM determination of the air-kerma rate

 $\overline{()}$

 u ^B represents the relative uncertainty estimated by other methods (Type B).

(2) Value adopted from January 2019 (Burns and Kessler 2018).

Table 4. X-rays (100 kV to 250 kV) Conditions of measurement at the BIPM

Distance between focal spot and reference plane of standard: 120 cm

Beam diameter in the reference plane: 9.8 cm

Inherent filtration: \approx 3 mm Be

Reference depth for absorbed dose measurement: 2 g $\rm cm^{-2}$

Reference qualities (1)

 (1) Recommended by Section I of the CCEMRI (1972).

(2) Mass attenuation coefficient for air.

Table 5. X-rays (100 kV to 250 kV)

Physical constants and correction factors used in the BIPM determination of the air-kerma rate (1) and absorbed-dose-to-water rate (2) and conversion factor from air kerma to absorbed dose to water

Dry air density (273.15 K, 101.325 kPa) = 1.2930 kg m⁻³

 $W/e = 33.97$ J C⁻¹

 $⁽¹⁾$ Details on the determination of the air-kerma rate are described by Boutillon (1978) and the re-evaluation of the</sup> correction factors is described by Burns *et al.* (2009).

⁽²⁾ Details on the determination of the absorbed-dose-to-water rate are described by Burns (2017).

⁽³⁾ Combined values for k_{ii} and k_{W} adopted from June 2017 for absorbed dose to water and from January 2019 for air kerma (Burns and Kessler 2018).

(4) Values at 293.15 K and 101.325 kPa for an attenuation length of 28.15 cm.

Table 6. X-rays (100 kV to 250 kV)

Estimated relative standard uncertainties in the BIPM determination of the air-kerma rate

and absorbed-dose-to-water rate

 μ ⁽¹⁾ μ _{iA} represents the relative uncertainty estimated by statistical methods (Type A);

 u_{iB} represents the relative uncertainty estimated by other methods (Type B).

⁽²⁾ Value adopted from June 2017 for absorbed dose to water and from January 2019 for air kerma (Burns and Kessler 2018).

Table 7. ⁶⁰Co gamma radiation Conditions of measurement at the BIPM

(1) The photon fluence rate at the centre of each side of the 10 cm \times 10 cm field is 50 % of the photon fluence rate at the centre of the square.

Table 8. 60Co gamma radiation

Physical constants and correction factors used in the BIPM determination of the air-kerma rate (1), and their estimated relative standard uncertainties

(1) Details on the determination of air kerma are described by Boutillon *et al.* (1973), Burns (2006), Burns *et al.* (2007) and the re-evaluation of the standard is described in Burns and Kessler (2018).

 μ ⁽²⁾ μ _{iA} represents the relative uncertainty estimated by statistical methods (Type A); u_{iB} represents the relative uncertainty estimated by other methods (Type B).

(3) Uncertainty value for the product *s*c,a *W*/*e* adopted from January 2019 (Burns and Kessler 2018).

⁽⁴⁾ The uncertainties for k_{wall} and k_{an} are included in the determination of the effective volume (Burns *et al.* 2007). (5) Standard CH6-2

(6) Over a period of 3 months. The long-term reproducibility over a period of 15 years, *u*rep, is 0.0004.

Table 9. 60Co gamma radiation

Physical constants and correction factors used in the BIPM ionometric determination of the absorbed-

dose-to-water rate (1) at 5 g cm[−]**² , and their estimated relative standard uncertainties**

(1) Details on the determination of absorbed dose to water are described by Boutillon *et al.* (1993) and the re-evaluation of the standard is described by Burns and Kessler (2018).

 μ ⁽²⁾ μ _{iA} represents the relative uncertainty estimated by statistical methods (Type A); u ^B represents the relative uncertainty estimated by other methods (Type B).

(3) Standard CH7-1.

(4) Over a period of 3 months. The long-term reproducibility over a period of 15 years, *u*rep, is 0.0006.

Table 10. MV-radiation beams Conditions of measurement at the DOSEO platform

Distance from effective source position to reference plane: 100 cm

Beam section in the reference plane: $10 \text{ cm} \times 10 \text{ cm}$

Reference depth for absorbed dose measurement: 10 g cm^{-2}

Reference qualities

Table 11. MV-radiation beams

Conversion and correction factors used in the BIPM calorimetric determination of the absorbed-dose-towater rate (1) at 10 g cm[−]**²**

(1) Details on the determination of the absorbed-dose rate are described in the BIPM.RI(I)-K6 comparison reports (Kessler *et al.* 2019, for example)

⁽²⁾ D_c absorbed dose to graphite, determined using the graphite calorimeter;

 $Q_{c,st}$ ionization charge measured by the standard chamber in the graphite phantom, corrected by $k_{s,st}$

Table 12. MV-radiation beams

Estimated relative standard uncertainties in the BIPM determination of absorbed dose to water (1)

Combined uncertainty of the BIPM determination of absorbed-dose-to-water rate

 $⁽¹⁾$ Details on the determination of absorbed dose to water are described in the BIPM.RI(I)-K6 comparison reports (Kessler</sup> *et al.* 2019, for example)

 $^{(2)}$ u_{iA} represents the relative uncertainty estimated by statistical methods (Type A); u_{iB} represents the relative uncertainty estimated by other methods (Type B).

⁽³⁾ D_c absorbed dose to graphite, determine using the graphite calorimeter;

 Q_c ionization charge measured by the standard chamber in the graphite phantom, corrected by k_s

Table 13. ¹³⁷Cs gamma radiation Conditions of measurement at the IAEA laboratories

Table 14. 137Cs gamma radiation

Physical constants and correction factors used in the BIPM determination of the air-kerma rate (1), and their estimated relative standard uncertainties

(1) Details on the determination of air kerma are described by Boutillon *et al.* (1996), Kessler *et al.* (2009) and the re-evaluation of the standard is described in Burns and Kessler (2018).

 μ ⁽²⁾ μ _{*iA*} represents the relative uncertainty estimated by statistical methods (Type A); u ^B represents the relative uncertainty estimated by other methods (Type B).

⁽³⁾ Uncertainty value for the product $s_{c,a}$ *W/e* adopted from January 2019 (Burns and Kessler 2018).

(4) Standard CH6-3

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