

# EURAMET Supplementary Comparison Measurement of groove depth standards in the range 1 µm up to 1 mm EURAMET.L-S26 EURAMET project 1407 Final Report

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## 1 Document control

| Version Draft A.2 | Issued on 4 <sup>th</sup> September 2019 |
|-------------------|--|
| Version Draft B   | Issued on 27 <sup>th</sup> February 2020 |
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## 2 Abstract

A comparison measurement between 10 national metrology institutes on two types of depth setting standards was conducted using mostly tactile but also two optical instruments for measurement. Three etched silicon standards with depths of 5, 20 and 50  $\mu$ m and one diamond turned nickel coated copper standard with depths of 200, 600 and 900  $\mu$ m were measured. The cross section of the grooves was trapezoidal. Most of the participants confirmed their CMC entries. Since many measurements had to be made, contamination of the standards and heavy wear on the standards were also observed after the comparison was completed. The wear consists of indentation marks from stylus instruments on both types of standards and as many as 70 scratch marks on the nickel coated copper artefact used. This indicates that the contact pressure of the tactile measuring devices used by some partners was too high. This can be caused by a too high probing force or a too small probing tip radius. Thus, for future comparisons the actual probing force and actual tip radius need to be measured during the comparison by the participants to assure that the recommended values (2  $\mu$ m tip radius and 0.7 mN probing force) are not exceeded. The recently published German standard DIN 32567-3 "Determination of the influence of materials on the optical and tactile dimensional metrology – Part 3: Derivation of correction values for tactile measuring devices" [1–3] describes methods to do both.

## 3 Introduction

The metrological equivalence of national measurement standards and of calibration certificates issued by national metrology institutes is established by a set of key and supplementary comparisons chosen and organized by the Consultative Committees of the CIPM or by the regional metrology organizations in collaboration with the Consultative Committees.

At its meeting in July 2016, the EURAMET Technical Committee for Length, TC-L, decided upon a supplementary comparison of groove depth standards in the range 1  $\mu$ m up to 1 mm, named EURAMET.L-S26, with PTB as the pilot laboratory. The comparison was registered in July 2016, artefact circulation started in September 2016 and was completed in October 2018.

## 4 Organization

#### 4.1 Participants

| Laboratory | Contact person, Laboratory                         | Phone, Fax, email               |
|------------|--|---------------------------------|
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 Table 1. List of participant laboratories and their contacts.

#### 4.2 Schedule

The participating laboratories were asked to specify a preferred timetable slot for their own measurements of the depth setting standards. The timetable given in table 2 has been drawn up taking these preferences into account. Each laboratory had six weeks that include customs clearance, calibration

and transportation to the following participant. With its confirmation to participate, each laboratory was obliged to perform the measurements in the allocated period and to allow enough time in advance for transportation so that the following participant receives them in time. If a laboratory had technical problems to perform the measurements or customs clearance took too long, the laboratory had to contact the pilot laboratory as soon as possible and, according to whatever it decides, it could eventually be obliged to send the standards directly to the next participant before completing the measurements or even without doing any measurements.

| RMO      | Laboratory | No. | Original<br>schedule    | Date of measurement     | Results<br>received |
|----------|------------|-----|-------------------------|-------------------------|---------------------|
| EURAMET  | РТВ        | 1   | 2016-09-01 – 2016-10-01 | September 2016          | -                   |
| COOMET   | VNIIMS     | 2   | 2016-10-01 – 2016-12-01 | October 2016            | 2017-04-10          |
| AFRIMETS | NMISA      | 3   | 2016-12-01 – 2017-02-01 | December 2016           | 2017-02-02          |
| EURAMET  | UME        | 4   | 2017-02-01 – 2017-04-01 | April 2016              | 2017-06-23          |
| Pilot    | РТВ        |     | 2017-04-01 – 2017-06-01 | -                       | -                   |
| EURAMET  | VTT        | 5   | 2017-06-01 2017-07-15   | June 2017               | 2017-08-24          |
| EURAMET  | BEV        | 6   | 2017-07-15 – 2017-09-01 | July 2017               | 2017-07-26          |
| EURAMET  | INRIM      | 7   | 2017-09-01 – 2017-10-15 | September 2017          | 2018-02-28          |
| EURAMET  | GUM        | 8   | 2017-10-15 – 2017-12-01 | November 2017           | 2018-01-12          |
| EURAMET  | CEM        | 9   | 2017-12-01 – 2018-02-01 | January 2018            | 2018-04-27          |
| Pilot    | РТВ        |     | 2018-02-01 – 2018-02-15 | -                       | -                   |
| EURAMET  | RISE       | 10  | 2018-02-15 - 2018-04-01 | March 2018              | 2018-05-09          |
| EURAMET  | BEV        | 11  | 2018-04-01 – 2018-05-15 | - 1                     | -                   |
| EURAMET  | VTT        | 12  | 2018-05-15 – 2018-07-01 | 2018-08-03 <sup>2</sup> | 2018-08-08          |
| Pilot    | РТВ        | 13  | 2018-07-01              | 2018-10-22              | 2018-10-29          |

Table 2. Schedule of the comparison.

<sup>1</sup> Cleaning of EN19\_7 <sup>2</sup> Second measurement

## 5 Artefacts

### 5.1 Description of artefacts

Four artefacts were used, three SiMetrics (SN 497, SN 499 and SN 502) and one PTB depth setting standard (EN19\_7). The depth setting standards contain v-shaped grooves of type A1 according to the standard ISO 5436-1:2000.

The coefficients of thermal expansion given in the following table are obtained by the manufacturers and should be used as such.

| Identification Nominal depth |   | fication Nominal depth Expansion coefficient /10 <sup>-6</sup> K <sup>-1</sup> |           |
|------------------------------|---|--|-----------|
| EN 19_7                      | EN 19_7 200 μm, 600 μm, 900 μm 16.6 ± 0.5 [4] |  | РТВ       |
| SN 497                       | SN 497 5 μm                                   |  | SiMetrics |
| SN 499                       | 20 µm   | 2.56 ± 0.5 [5]   | SiMetrics |
| SN 502                       | 50 µm   | 2.56 ± 0.5 [5]   | SiMetrics |

Table 3. List of artefacts.

#### 5.2 Gradient of groove depth

Three profile sections (a, b and c) at distances of 0.5 mm for the standards SN 497, SN 499 and SN502 and at distances of 1 mm on the standard EN19\_7 had to be measured three times (see 6.1). From these measurements an average groove depth was calculated. To estimate the constancy of the groove depth at different positions, the groove depths measured by PTB were plotted in Fig. 1-6 and the spread of the groove depths at different positions was determined. The spread of the averaged groove depths varies between 12 nm (20  $\mu$ m and 200  $\mu$ m groove) and 22 nm (600  $\mu$ m groove) and only for the 50  $\mu$ m groove a clear gradient of the groove depth of 66 nm/mm could be observed.



Figure 1 Measured groove depths at different measurement positions (section a: y = -0.5 mm, section b: y = 0 and section c: y = 0.5 mm) on the standard SN 497.

Figure 2 Measured groove depths at different measurement positions (section a: y = -0.5 mm, section b: y = 0 and section c: y = 0.5 mm) on the standard SN 499.



Figure 3MeasuredgroovedepthsatdifferentFigure 4measurement positions (section a: y = -0.5 mm, section b:measurementy = 0 and section c: y = 0.5 mm) on the standard SN 502.y = 0 and section c:



200,000 2nd meas 199,995 3rd meas ШШ Mean val Groove depth in 199,990 199,985 199,980 199,975 -1 -0.8 -0.6 -0.4 -0.2 0 0.2 0.4 0.6 0.8 y-Position in mm

**Figure 4** Measured groove depths at different measurement positions (section a: y = -1 mm, section b: y = 0 and section c: y = 1 mm) for the 200 µm groove on the standard EN19\_7.



**Figure 5** Measured groove depths at different measurement positions (section a: y = -1 mm, section b: y = 0 and section c: y = 1 mm) for the 600  $\mu$ m groove on the standard EN19\_7.

**Figure 6** Measured groove depths at different measurement positions (section a: y = -1 mm, section b: y = 0 and section c: y = 1 mm) for the 900 µm groove on the standard EN19\_7.

#### 5.3 Condition of artefacts at start/end of comparison

The condition of the artefact's measurement surfaces was measured by optical microscopy before start of the comparison (see Figures 7, 9, 11, 13, 15 and 17) and after the comparison (see Figures 8,10,12,14,16 and 18). Although the participants were asked to check the condition of the artefact surfaces prior to and after measurements, only the participants who measured optically, carefully investigated the condition of the artefacts and reported contamination (see Figure 19 to Figure 22) and scratching (Figure 23) of the artefacts.



Figure 7 Microscope image of 5  $\mu$ m groove before comparison measurements.

Figure 8 Microscope image of 5  $\mu$ m groove after comparison measurements. The spots on the right side are marks, probably caused by diamond stylus.



Figure 9 Microscope image of 20  $\mu m$  groove before comparison measurements.



Figure 10 Microscope image of 20  $\mu m$  groove after comparison measurements. The spots on the right side are marks, probably caused by diamond stylus.



Figure 11 Microscope image of 50  $\mu m$  groove before comparison measurements.



Figure 12 Microscope image of region "A" of 50  $\mu$ m groove after comparison measurements. The white spots are marks, probably caused by a stylus instrument.



Figure 13 Microscope image of 200  $\mu m$  groove before comparison measurements



Figure 14 Microscope image of 200 µm groove after comparison measurements



Figure 15 Microscope image of 600  $\mu m$  groove before comparison measurements



Figure 17 Microscope image of 900 µm groove before comparison measurements

Figure 18 Microscope image of 900 µm groove after comparison measurements

The artefacts were not cleaned prior to the measurements. They were new and not used at the start of the comparison. No scratches and only a few contamination particles could be observed on the surfaces (see Fig. 7, 9, 11, 13, 15 and 17). During the comparison a contamination, mainly of the artefact EN19\_7 containing the deeper grooves, could be observed (see Figure 19 and Figure 21)



Figure 16 Microscope image of 600 µm groove after



Since the contamination of the artefact could cause considerable measurement deviations, it was decided to clean the artefact at the end of the comparison and to repeat the optical measurements. BEV cleaned the samples and most of the contamination could be removed (see Figure 22). The cleaning procedure is described in Appendix D.

Unfortunately, due to technical problems BEV was not able to measure again, but VTT measured all artefacts again. Thus, VTT's second measurement was included in the comparison. The change in VTT's measurement results is shown in Figure 20.



**Figure 19** Contaminated artefact EN19\_7 containing the three deeper grooves after all partners performed their measurements.

It can be concluded that the deviation of VTT's measurements from the reference values were significantly reduced only for the 200  $\mu$ m groove. Before cleaning a deviation of 62 nm and after cleaning a deviation of only -25 nm was observed at a stated expanded uncertainty of VTT for this groove depth of 58 nm.

Thus, cleaning led to a maximum change in measured groove depth of -87 nm.



**Figure 20** Deviation of VTT's first measurement (blue) and second measurement (red) after cleaning of the artefact EN19\_7 with the three deepest grooves.

As expected, the three smaller grooves depths stay constant in depth, while the three deeper groove depths changed after cleaning (see Figure 20). The deviation from the reference value decreased for the 200  $\mu$ m and 900  $\mu$ m grooves, while the deviation of the 600  $\mu$ m groove slightly increased.



**Figure 21** Contamination of artefact EN19\_7 **Figure 22** Condition of artefact containing the three deeper grooves.

Figure 22 Condition of artefact EN19\_7 after cleaning.

Beyond contamination of the artefacts, scratching seems to be a major problem for most of the tactile instruments. Figure 23 shows a microscope image of artefact EN19\_7 after all partners had taken their measurements. As many as 70 scratching marks can be counted in Figure 23.



Figure 23 Microscope DIC image of artefact EN19\_7 showing the huge number of scratches produced by tactile measurements.

Thus, most of the participants who measured with a stylus instrument used too high probing forces which led to a scratching of the Nickel surface of artefact EN19\_7. The surface of the Silicon artefacts was also investigated for scratching tracks, but on these much harder surfaces the tracks look different. There are no continuous scratch marks to be seen, but individual holes to be recognized (see Figure 24 - Figure 27).



**Figure 24** Microscope DIC image of artefact SN497 in the range of the left markers showing several defects on the surface resulting from tactile measurements.



Figure 26 Microscope DIC image of artefact SN499 showing several defects on the surface resulting from tactile measurements.



**Figure 25** Microscope DIC image of artefact SN497 in the range of the right markers showing several defects on the surface resulting from tactile measurements.



**Figure 27** Microscope DIC image of artefact SN502 showing several defects on the surface resulting from tactile measurements.

## 6 Measuring instructions

#### 6.1 Measurands

The depth setting standards were measured based on the standard procedure that the laboratory regularly uses for this calibration service for its customers.

#### 6.1.1 PTB depth setting standard EN19\_7

The PTB 900  $\mu$ m depth setting standard contains seven grooves and two alignment grooves with a depth of 450  $\mu$ m (see Figure 28 and Figure 29). For instruments with a z-measurement range of only 1 mm the alignment grooves allow to align the zero value in z-direction by probing in one of the two alignment grooves.



Figure 28 Photo of the 900  $\mu m$  PTB depth setting standard EN19\_7



**Figure 29** Evaluation of the groove depth *d* according to ISO 5436-1 (dimensions in mm)



Figure 30 Depiction of the three profiles (a, b, c) to be measured on the 900  $\mu m$  PTB standard and the location of the grooves on the standard

Only the depths of the three grooves with the nominal depths of 200  $\mu m$  , 600  $\mu m$  and 900  $\mu m$  had to be measured.

Three parallel profiles ("a, b, c" see Figure 30) in the middle of the standard separated by a distance of 1 mm were measured. This procedure had to be repeated two times in order to obtain nine profiles. The measurand was the groove depth d which had to be determined for each profile according to ISO 5436-1 [6] (see Figure 30) but with a fixed groove width of 300 µm. Thus, for tilt correction the two profile sections between the marks 1 and 2 ("A") and between the marks 5 and 6 ("B") should have a distance from the upper groove edges of 0.1 mm. After tilt correction the groove depth d has to be determined as the mean value of the profile section "C" between the marks 3 and 4. This profile section should have a length of 0.1 mm.

The arithmetic mean of all nine groove depths was the measurand to be reported.

The ASCII data of the nine profiles measured for each groove had to be attached to the final report and the file names had to be listed in the report form.

#### 6.1.2 SiMetrics depth setting standards

The SiMetrics depth setting standards consist of a 50 mm x 50 mm glass plate on which the depth setting standard silicon chips are bonded (see Figure 31).

Three parallel profiles ("a, b, c" see Figure 33) separated by a distance of 0.5 mm were measured. This procedure had to be repeated two times in order to obtain nine profiles. The measurand is the groove depth d which has to be determined for each profile according to ISO 5436-1 [6] (see Figure 32). For tilt correction the two profile sections between the marks 1 and 2 ("A") and between the marks 5 and 6 ("B") should have a distance from the upper groove edges of 0.1 mm. After tilt correction the groove depth d has to be determined as the mean value of the profile section between the marks 3 and 4. This profile section "C" has a width of one third of the groove width w. The following groove widths w should be used:

| Depth<br>setting<br>standard | nominal<br>groove<br>depth<br>μm | groove<br>width<br>w / mm | <i>length of<br/>"C"</i><br>w/3<br>mm |
|------------------------------|----------------------------------|---------------------------|---------------------------------------|
| SN 497                       | 5                                | 1.772                     | 0.591                                 |
| SN 499                       | 20                               | 1.749                     | 0.583                                 |
| SN 502                       | 50                               | 1.708                     | 0.569                                 |
| EN19_7                       | 200, 600,<br>900                 | 0.300                     | 0.100                                 |

**Table 4.** List of groove widths for the evaluation of the groove depth.

The arithmetic mean of the three groove depths for each section ("a, b, c") is the measurand to be reported.

The ASCII data of the nine profiles measured for each groove had to be attached to the final report and the file names had to be listed in the report form.



**Figure 31** The SiMetrics depth setting standards consist of a glass plate with the bonded silicon chip on it and an engraved serial number



**Figure 32** Evaluation of the groove depth *d* for the SiMetrics grooves according to ISO 5436-1 (dimensions in mm)



**Figure 33** Depiction of the SiMetrics depth setting standards and the location of three profiles (a, b, c) to be measured

## 7 Results

#### 7.1 Measurement uncertainties

The uncertainty of measurement should be estimated according to the ISO *Guide to the Expression of Uncertainty in Measurement*. The participating laboratories are encouraged to use all known influence parameters for the method applied by them. The groove depth d of the standards is expressed as a function of the input quantities  $x_i$ 

$$d = f(x_i) \tag{1}$$

The combined standard uncertainty  $u_c(d)$  is the square sum of the standard uncertainties of the input quantities  $u(x_i)$ , each weighted by a sensitivity coefficient  $c_i$ 

$$u_c^2(h) = \sum_i c_i^2 u^2(x_i) \text{ with } c_i = \frac{\partial h}{\partial x_i}$$
(2)

Since the MRA requires that participants submit results supported by a full uncertainty calculation, the participants were requested to report their measurement uncertainty budget in a table (see appendix C) whose format corresponds with the scheme below:

| Quantity | Estimate | Standard                           | Probability  | Sensitivity | Uncertainty        | Degrees of |
|----------|----------|------------------------------------|--------------|-------------|--------------------|------------|
|          |          | uncertainty                        | distribution | coefficient | contribution       | freedom    |
| Xi       | Xi       | <i>u</i> ( <i>x</i> <sub>i</sub> ) |              | Ci          | u <sub>i</sub> (h) | Vi         |
|          |          |                                    |              |             |                    |            |

For the type of probability distribution please use: N = normal; R = rectangular; T = triangular; U = U-shaped.

Alternatively, participants were asked to simply submit an overall uncertainty value. Ideally, for rangebased CMCs, the participant could submit both an uncertainty expression plus a value for each measurand.

As well as stating a measurement uncertainty for each measurand, the participant should also state the calculated or assumed degrees of freedom.

#### 7.2 Changes to results after Draft A.1

VNIIMS uncertainty data had to be changed. In the sensor nonlinearity instead of "mm" the unit " $\mu$ m" was used leading to too large uncertainty contributions. This was changed in the version Draft A.2.

GUM had reported expanded uncertainties instead of standard uncertainties. This led to only small changes of the reference value. This was changed in the version Draft B.

## 8 Analysis

#### 8.1 Calculation of the KCRV

The weighted mean was the KCRV for each measurand. Before the weights could be assigned and the mean taken, it was necessary to exclude any clear outliers from the analysis. The analysis for each measurand proceeds as follows:

We assume the total number of participants submitting a result is *I*.

Each laboratory reports a measured value,  $x_i$ , and its associated standard uncertainty  $u(x_i)$ .

<ITERATION START> Compute the normalised weight,  $w_i$ , for the result  $x_i$  is given by:

$$w_i = C \cdot \frac{1}{[u(x_i)]^2}$$
(1)

where the normalising factor, *C*, is given by:

$$C = \frac{1}{\sum_{i=1}^{I} \left(\frac{1}{u(x_i)}\right)^2} \tag{2}$$

Then calculate the weighted mean,  $\bar{x}_w$ , which is given by:

$$\bar{x}_w = \sum_{i=1}^{I} w_i \cdot x_i \tag{3}$$

The uncertainty of the weighted mean is calculated by:

$$u(\bar{x}_w) = \sqrt{\frac{1}{\sum_{i=1}^{I} \left(\frac{1}{u(x_i)}\right)^2}} = \sqrt{C}$$
(4)

After deriving the weighted mean and its associated standard uncertainty, the deviation of each laboratory's result from the weighted mean is determined simply as  $x_i - \bar{x}_w$ . The uncertainty of this deviation is calculated as a combination of the uncertainties of the result,  $u(x_i)$ , and the uncertainty of the weighted mean  $u(\bar{x}_w)$ . The uncertainty of the deviation from the weighted mean is given by equation (5), which includes a minus sign to take into account the correlation between the two uncertainties (it

would be a plus sign if dealing with uncorrelated uncertainties, such as when comparing data from two separate laboratories).

$$u(x_i - \bar{x}_w) = \sqrt{[u(x_i)]^2 - [u(\bar{x}_w)]^2}$$
(5)

For the determination of the key comparison reference value KCRV, statistical consistency of the results contributing to the KCRV is required. A check for statistical consistency of the results with their associated uncertainties can be made by calculating the E<sub>n</sub> value for each laboratory's result, where E<sub>n</sub> is defined as the ratio of the deviation from the weighted mean, divided by the expanded uncertainty of this deviation:

$$E_n = \frac{x_i - \bar{x}_w}{2\sqrt{[u(x_i)]^2 - [u(\bar{x}_w)]^2}}$$
(6)

The results are examined and any result for which  $|E_n| > 1$  is considered as an inconsistent result. Identify the result with the largest  $|E_n|$ , go back to <ITERATION START> and repeat the analysis, but excluding this result from contributing to the weighted mean – *i.e.* they have a weighting of zero. Because inconsistent results are no longer correlated with the weighted mean, when calculating their deviation from the weighted mean, and when calculating their  $E_n$  value, a positive sign is used in equation (5) and consequently in the denominator of equation (6).

This process is iterated until there are no inconsistent results contributing to the weighted mean. After reaching consistency, the calculated weighted mean is the KCRV (see Table 5 -Table 10).

Figure 34 - Figure 39 show the measured depth values and expanded uncertainties in comparison to the weighted mean (red lines) and their uncertainties (red dotted lines).





expanded uncertainty of KCRV).





Figure 36 Measured depth values of the participants for the 200  $\mu$ m groove (red line: KCRV, dotted red lines: expanded uncertainty of KCRV).



**Figure 37** Measured depth values of the participants for the 50  $\mu$ m groove (red line: KCRV, dotted red lines: expanded uncertainty of KCRV).



Figure 38 Measured depth values of the participants for the 20  $\mu m$  groove (red line: KCRV, dotted red lines: expanded uncertainty of KCRV).



Figure 39 Measured depth values of the participants for the 5  $\mu$ m groove (red line: KCRV, dotted red lines: expanded uncertainty of KCRV).

#### 8.2 Calculation of Degrees of Equivalence

The Degree of Equivalence, DoE, for a laboratory result  $x_i$  is calculated simply as  $x_i - \bar{x}_w$ . The uncertainty of the DoE is calculated using either

$$u(x_i - \bar{x}_w) = \sqrt{[u(x_i)]^2 - [u(\bar{x}_w)]^2}$$
 for results which contributed to the weighted mean

or  $u(x_i - \bar{x}_w) = \sqrt{[u(x_i)]^2 + [u(\bar{x}_w)]^2}$  for results which made no contribution. The tables 5-10 show the measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and the contribution to the mean value and to the weighted mean for all six groove depths.

**Table 5.** 900 µm groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean (\*: no measurement available).

| 900 µm      | <b>X</b> i | <i>u(x</i> i) | <i>U</i> ( <i>x</i> <sub>i</sub> ) | En   | $(x_i - \bar{x}_w)$ | $U(x_i - $        | Contribu- |
|-------------|------------|---------------|------------------------------------|------|---------------------|-------------------|-----------|
|             |            |               |                                    |      |                     | $(x_w)U(x_i-x_w)$ | tion to   |
|             | μm         | μm            | μm                                 |      | μm                  | μm                | ref. val. |
| РТВ         | 899.884    | 0.027         | 0.054                              | 0.42 | -0.020              | 0.048             | Y         |
| VNIIMS      | 899.825    | 0.049         | 0.098                              | 0.84 | -0.079              | 0.095             | Y         |
| NMISA       | 899.907    | 0.049         | 0.097                              | 0.03 | 0.003               | 0.094             | Y         |
| UME         | 900.156    | 0.061         | 0.123                              | 2.01 | 0.252               | 0.125             | Ν         |
| RISE        | 899.650    | 4.160         | 8.320                              | 0.03 | -0.254              | 8.320             | Y         |
| BEV         | 899.919    | 0.016         | 0.032                              | 0.76 | 0.015               | 0.019             | Y         |
| INRIM       | 899.960    | 0.210         | 0.420                              | 0.13 | 0.056               | 0.419             | Y         |
| GUM         | 900.504    | 0.527         | 1.054                              | 0.57 | 0.600               | 1.054             | Y         |
| CEM         | *          | *             | *                                  | *    | *                   | *                 | *         |
| VTT 2nd     | 899.870    | 0.130         | 0.260                              | 0.13 | -0.034              | 0.259             | Y         |
| Mean value  | 899.940    |               |                                    |      |                     |                   |           |
| Stand. dev. | 0.231      |               |                                    |      |                     |                   |           |
| Ref. value  | 899.904    |               |                                    |      |                     |                   |           |
| Uncertainty | 0.025      |               |                                    |      |                     |                   |           |

**Table 6.** 600 µm groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean (\*: no measurement available).

| 600 μm      | Xi      | <i>u</i> ( <i>x</i> <sub>i</sub> ) | <i>U</i> ( <i>x</i> <sub>i</sub> ) | En    | $(x_i - \bar{x}_w)$ | $U(x_i - \bar{x}_w)U(x_i - \bar{x}_w)$ | Contribu-<br>tion to |
|-------------|---------|------------------------------------|------------------------------------|-------|---------------------|--|----------------------|
|             | μm      | μm                                 | μm                                 |       | μm                  | μm                                     | ref. val.            |
| РТВ         | 599.913 | 0.022                              | 0.044                              | 0.12  | -0.004              | 0.037                                  | Y                    |
| VNIIMS      | 599.893 | 0.045                              | 0.090                              | 0.28  | -0.024              | 0.087                                  | Y                    |
| NMISA       | 599.931 | 0.044                              | 0.088                              | 0.16  | 0.014               | 0.085                                  | Y                    |
| UME         | 601.287 | 0.052                              | 0.104                              | 12.82 | 1.370               | 0.107                                  | Ν                    |
| RISE        | 599.810 | 2.770                              | 5.540                              | 0.02  | -0.107              | 5.540                                  | Y                    |
| BEV         | 599.921 | 0.016                              | 0.032                              | 0.17  | 0.004               | 0.022                                  | Y                    |
| INRIM       | 599.960 | 0.160                              | 0.320                              | 0.13  | 0.043               | 0.319                                  | Y                    |
| GUM         | 599.437 | 0.351                              | 0.702                              | 0.68  | -0.480              | 0.702                                  | Y                    |
| CEM         | *       | *                                  | *                                  | *     | *                   | *                                      | *                    |
| VTT 2nd     | 599.934 | 0.087                              | 0.174                              | 0.10  | 0.017               | 0.172                                  | Y                    |
| Mean value  | 599.850 |                                    |                                    |       |                     |  |                      |
| Stand. dev. | 0.162   |                                    |                                    |       |                     |  |                      |
| Ref. value  | 599.917 |                                    |                                    |       |                     |  |                      |
| Uncertainty | 0.024   |                                    |                                    |       |                     |  |                      |

| 200 µm      | Xi      | <i>u</i> ( <i>x</i> <sub>i</sub> ) | <i>U</i> ( <i>x</i> <sub>i</sub> ) | En    | $(x_i - \bar{x}_w)$ | $U(x_i - \bar{x}_w)U(x_i - \bar{x}_w)$ | Contribu-<br>tion to |
|-------------|---------|------------------------------------|------------------------------------|-------|---------------------|--|----------------------|
|             | μm      | μm                                 | μm                                 |       | μm                  | μm                                     | ref. val.            |
| РТВ         | 199.989 | 0.015                              | 0.029                              | 0.78  | 0.019               | 0.024                                  | Y                    |
| VNIIMS      | 199.956 | 0.039                              | 0.078                              | 0.19  | -0.014              | 0.076                                  | Y                    |
| NMISA       | 199.971 | 0.038                              | 0.076                              | 0.01  | 0.001               | 0.074                                  | Y                    |
| UME         | 201.039 | 0.034                              | 0.067                              | 15.50 | 1.069               | 0.069                                  | Ν                    |
| RISE        | 199.970 | 0.920                              | 1.840                              | 0.00  | 0.000               | 1.840                                  | Y                    |
| BEV         | 199.965 | 0.016                              | 0.032                              | 0.18  | -0.005              | 0.028                                  | Y                    |
| INRIM       | 199.910 | 0.080                              | 0.160                              | 0.38  | -0.060              | 0.159                                  | Y                    |
| GUM         | 199.949 | 0.127                              | 0.254                              | 0.08  | -0.021              | 0.253                                  | Y                    |
| CEM         | 199.965 | 0.016                              | 0.032                              | 0.19  | -0.005              | 0.028                                  | Y                    |
| VTT 2nd     | 199.945 | 0.029                              | 0.058                              | 0.45  | -0.025              | 0.056                                  | Y                    |
| Mean value  | 199.958 |                                    |                                    |       |                     |  |                      |
| Stand. dev. | 0.021   |                                    |                                    |       |                     |  |                      |
| Ref. value  | 199.970 |                                    |                                    |       |                     |  |                      |
| Uncertainty | 0.016   |                                    |                                    |       |                     |  |                      |

**Table 7.** 200 µm groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean.

**Table 8.** 50 µm groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean.

| 50 µm       | Xi     | <i>u</i> ( <i>x</i> <sub>i</sub> ) | <i>U</i> ( <i>x</i> <sub>i</sub> ) | En   | $(x_i - \bar{x}_w)$ | $U(x_i - \bar{x}_w)U(x_i - \bar{x}_w)$ | Contribu- |
|-------------|--------|------------------------------------|------------------------------------|------|---------------------|--|-----------|
|             | μm     | μm                                 | μm                                 |      | μm                  | μm                                     | mean      |
| РТВ         | 50.274 | 0.013                              | 0.026                              | 0.24 | 0.005               | 0.022                                  | Y         |
| VNIIMS      | 50.269 | 0.037                              | 0.074                              | 0.00 | 0.000               | 0.073                                  | Y         |
| NMISA       | 50.266 | 0.044                              | 0.087                              | 0.03 | -0.003              | 0.086                                  | Y         |
| UME         | 50.245 | 0.024                              | 0.048                              | 0.53 | -0.024              | 0.046                                  | Y         |
| RISE        | 50.273 | 0.233                              | 0.466                              | 0.01 | 0.004               | 0.466                                  | Y         |
| BEV         | 50.270 | 0.026                              | 0.052                              | 0.02 | 0.001               | 0.050                                  | Y         |
| INRIM       | 50.240 | 0.070                              | 0.140                              | 0.21 | -0.029              | 0.139                                  | Y         |
| GUM         | 50.220 | 0.034                              | 0.068                              | 0.74 | -0.049              | 0.066                                  | Y         |
| CEM         | 50.277 | 0.012                              | 0.023                              | 0.45 | 0.008               | 0.018                                  | Y         |
| VTT 2nd     | 50.351 | 0.008                              | 0.016                              | 3.81 | 0.082               | 0.022                                  | Ν         |
| Mean value  | 50.259 |                                    |                                    |      |                     |  |           |
| Stand. dev. | 0.019  |                                    |                                    |      |                     |  |           |
| Ref. value  | 50.269 |                                    |                                    |      |                     |  |           |
| Uncertainty | 0.015  |                                    |                                    |      |                     |  |           |

**Table 9.** 20  $\mu$ m groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean.

| 20 um       | Xi     | <i>u</i> ( <i>x</i> <sub>i</sub> ) | <i>U</i> ( <i>x</i> <sub>i</sub> ) | En   | $(x_i - \bar{x}_w)$ | $U(x_i - \overline{x}_i)$ | Contribu- |
|-------------|--------|------------------------------------|------------------------------------|------|---------------------|---------------------------|-----------|
| 20 µ        |        |                                    |                                    |      |                     | $x_w$ )U( $x_i$ - $x_w$ ) | tion to   |
|             | μm     | μm                                 | μm                                 |      | μm                  | μm                        | mean      |
| РТВ         | 21.900 | 0.012                              | 0.023                              | 0.21 | 0.005               | 0.022                     | Y         |
| VNIIMS      | 21.896 | 0.037                              | 0.074                              | 0.01 | 0.001               | 0.073                     | Y         |
| NMISA       | 21.897 | 0.036                              | 0.071                              | 0.02 | 0.002               | 0.071                     | Y         |
| UME         | 21.886 | 0.024                              | 0.049                              | 0.20 | -0.010              | 0.048                     | Y         |
| RISE        | 21.882 | 0.103                              | 0.206                              | 0.06 | -0.013              | 0.206                     | Y         |
| BEV         | 21.896 | 0.004                              | 0.009                              | 0.11 | 0.001               | 0.006                     | Y         |
| INRIM       | 21.880 | 0.070                              | 0.140                              | 0.11 | -0.015              | 0.140                     | Y         |
| GUM         | 21.873 | 0.017                              | 0.034                              | 0.67 | -0.022              | 0.033                     | Y         |
| CEM         | 21.896 | 0.005                              | 0.011                              | 0.09 | 0.001               | 0.009                     | Y         |
| VTT 2nd     | 21.948 | 0.005                              | 0.009                              | 4.82 | 0.053               | 0.011                     | Ν         |
| Mean value  | 21.890 |                                    |                                    |      |                     |                           |           |
| Stand. dev. | 0.009  |                                    |                                    |      |                     |                           |           |
| Ref. value  | 21.895 |                                    |                                    |      |                     |                           |           |
| Uncertainty | 0.006  |                                    |                                    |      |                     |                           |           |

**Table 10.** 5 µm groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean.

| 5 μm        | <b>X</b> i | <i>u</i> ( <i>x</i> <sub>i</sub> ) | <i>U</i> ( <i>x</i> <sub>i</sub> ) | En   | $(x_i - \bar{x}_w)$ | $U(x_i - \bar{x}_i) U(x_i - \bar{x}_i)$ | Contribu- |
|-------------|------------|------------------------------------|------------------------------------|------|---------------------|---|-----------|
|             |            |                                    |                                    |      |                     | $\chi_W = (\Lambda_1 - \Lambda_W)$      | tion to   |
|             | μm         | μm                                 | μm                                 |      | μm                  | μm                                      | mean      |
| РТВ         | 5.050      | 0.011                              | 0.022                              | 0.04 | -0.001              | 0.021                                   | Y         |
| VNIIMS      | 5.035      | 0.037                              | 0.073                              | 0.22 | -0.016              | 0.073                                   | Y         |
| NMISA       | 5.047      | 0.036                              | 0.071                              | 0.05 | -0.004              | 0.071                                   | Y         |
| UME         | 5.054      | 0.021                              | 0.041                              | 0.06 | 0.003               | 0.041                                   | Y         |
| RISE        | 5.045      | 0.029                              | 0.058                              | 0.10 | -0.006              | 0.058                                   | Y         |
| BEV         | 5.051      | 0.005                              | 0.011                              | 0.02 | 0.000               | 0.009                                   | Y         |
| INRIM       | 5.120      | 0.050                              | 0.100                              | 0.69 | 0.069               | 0.100                                   | Y         |
| GUM         | 5.049      | 0.017                              | 0.034                              | 0.06 | -0.002              | 0.033                                   | Y         |
| CEM         | 5.051      | 0.005                              | 0.009                              | 0.02 | 0.000               | 0.007                                   | Y         |
| VTT 2       | 5.062      | 0.004                              | 0.007                              | 1.16 | 0.011               | 0.010                                   | Ν         |
| Mean value  | 5.056      |                                    |                                    |      |                     |   |           |
| Stand. dev. | 0.023      |                                    |                                    |      |                     |   |           |
| Ref. value  | 5.051      |                                    |                                    |      |                     |   |           |
| Uncertainty | 0.006      |                                    |                                    |      |                     |   |           |

#### 8.3 Discussion of results

Outliers that had to be excluded from contributing to the KCRV (weighted mean) are:

• from UME for the groove depths 900/600/200 μm,

• from VTT for the groove depths  $50/20/5 \ \mu m$ .

UME used a smaller uncertainty in the comparison than the one stated in their existing CMC entry. This led to the systematic outliers for the three deeper grooves (200/600/900  $\mu$ m). Nevertheless, the existing CMC entry stating higher uncertainties (Q[33,13*d*] (*d* in  $\mu$ m)) is confirmed by UME's measurements in this comparison.

UME used their new roughness measurement device MarSurf XCR-20 for the first time in this intercomparison. The uncertainty U = Q[33; 13d] nm (with d in  $\mu$ m) in UMEs CMC entry belongs to their old roughness measurement device Mahr Perthometer Concept (produced in 1995). UME thought to achieve more precise results in the comparison using their new device. Indeed, good results were obtained in the 0 - 50  $\mu$ m range, but since they didn't have groove depth standards beyond 50  $\mu$ m, they were not able to obtain precise measurements in the 50 - 1000  $\mu$ m range. A PTB calibrated groove depth standard with 8 grooves whose depths are varying from 1  $\mu$ m to 900  $\mu$ m was used as a reference depth standard for all measurements in the comparison. The cross sections of the grooves are trapezoid. The grooves whose nominal depths are 5  $\mu$ m, 20  $\mu$ m, 50  $\mu$ m, 600  $\mu$ m and 900  $\mu$ m were used to calculate calibration factors on this reference standard. In the comparison, for the grooves which are < 0.1 (see Table 8, Table 9 and Table 10). UME currently has not yet understood the cause of the deviations for the 900/600/200  $\mu$ m grooves. The problem may be caused by the long probe arm which is used for the measurement of the 900/600/200  $\mu$ m grooves. Or it may be caused by not calibrating the device at the same day as the intercomparison measurements.

In future UME intends to decrease their CMC uncertainty in the 0.01 - 50  $\mu$ m range to U = Q[38, 3d] nm (with d in  $\mu$ m) which is larger than both the UME deviation from the weighted average and the UME uncertainty given in the intercomparison. For the range 51 - 900  $\mu$ m, UME intends not to apply for a CMC entry under the current condition of their stylus instrument, until they resolve the issue about their measurement system and procedure.

VTT measured optically using a Bruker GT-K optical 3D profiler (coherence scanning interferometer) with a 2.5x magnification objective, a 0.55x secondary lens and a pixel size of 7.1  $\mu$ m. For this instrument no CMC entry exists. The stated expanded uncertainty for these measurements was Q[23.4, 35.6*d*] with *d* in  $\mu$ m. The three outliers could be explained by a contamination of the silicon artefacts, since only the artefact EN19\_7 (900/600/200  $\mu$ m) but not the silicon artefacts were cleaned before VTT measured again (VTT 2nd). Another reason for the observed deviations is that VTT did not have good calibration samples for heights between 1  $\mu$ m and 500  $\mu$ m at the time of the comparison. The optical instrument used, currently has no CMC entry, but the entry was requested. This service will be greyed out when it is published until all corrective actions are performed.

After the comparison only a few marks were found on the surfaces of the three silicon artefacts, but as many as 70 scratch marks on the nickel coated copper artefact EN19\_7. This indicates that the contact pressure used for the measurements was too high for many participants. This can be caused by a too high probing force or a too small probing tip radius. Thus, for future comparisons the actual probing force and actual tip radius need to be measured during the comparison by the participants to assure that the values recommend (2  $\mu$ m tip radius and 0.7 mN probing force [4]) are not exceeded. The recently published German standard DIN 32567-3 "Production equipment for microsystems – Determination of the influence of materials on the optical and tactile dimensional metrology – Part 3: Derivation of correction values for tactile measuring devices" describes methods to do both.

#### 8.4 Linking of result to other comparisons

There is no need in linking Supplementary Comparisons.

This was the first EURAMET comparison on depth setting standards up to 1 mm depth. Previous comparisons on smaller depth setting standards are:

- EUROMET.L-S3 (Depth Setting Standards) up to depths of 3.2 µm, published in 1997 [7]
- EUROMET.L-S11 (Surface Texture) up to depths of 8 μm, published in 2004 [8]
- EUROMET.L-S15 (Step Height Standards) up to depths of 2 µm, published in 2006 [9]
- EUROMET.L-S15.a (Step Height Standards and 1D Gratings) up to depths of 2 µm, published in 2009 [8]
- APMP.L-K8 2008-2010 with groove depth sizes of 0.4  $\mu$ m to 10  $\mu$ m [9]

- EURAMET.L-K8.2013 (Surface Roughness Standards) where an A2-standard with depths down to 9  $\mu m$  was one of the artefacts [10].

## 9 Appendix A Equipment and measuring uncertainties of the participants

A wide range of equipment has been used. Therefore, this appendix describes the equipment

Table 11 Equipment and measuring uncertainties of the participants

| Partici-<br>pant | Instruments used   | Probing<br>force (μN) | Tip<br>radius/<br>lateral<br>resolution<br>(μm) | Cone<br>angle<br>of tip<br>(°) | Traverse<br>speed<br>(μm/s) | Traceability of<br>z-axis   | CMC entry for<br>depths from d <sub>min</sub> to<br>d <sub>max</sub><br>d <sub>min</sub> d <sub>max</sub> | Expanded uncertainty <i>U</i><br>(nm)  |
|------------------|--|-----------------------|---|--------------------------------|-----------------------------|---|---|--|
| РТВ              | Stylus instrument Mahr Surf<br>LD120                                 | 500                   | 2   | 60                             | 100                         | Depth setting<br>standards<br>traceable to<br>laser inter-<br>ferometry             | 0.1 μm 5 mm   | Q[22,36 <i>d</i> ] ( <i>d</i> in mm)   |
| BEV              | Nano measuring machine<br>SIOS NMM-1-0016 with laser<br>focus sensor | 0                     | -   | -                              | 20/50                       | Laser interfero-<br>meter   | 0.01 μm 10 μm   | Q[5,10 <i>d</i> ] ( <i>d</i> in μm) (**)<br>Published CMC<br>uncertainty for a different<br>instrument |
| CEM              | KLA Tencor P-6 Stylus Profiler                                       | 20                    | 2   | 60                             | 50, 100                     | Depth setting<br>standards<br>traceable to<br>laser<br>interferometry<br>(SIOS NMM) | 0.01 μm 15 μm   | Q[2,20 <i>d</i> ] ( <i>d</i> in μm)  |

| GUM    | Form Talysurf i-Series contact profilometer                  | 1000     | 2   |    | 500 | Depth setting<br>standard<br>calibrated by<br>PTB   | 0.1 μm 100 μm      | Q[30,0.5 <i>d</i> ] ( <i>d</i> in μm)   |
|--------|--|----------|-----|----|-----|---|--------------------|---|
| INRIM  | Talysurf II stylus profilometer<br>with interferometric head | 1000     | 2.5 | 90 | 500 | Reference<br>sphere, gauge<br>block step<br>heights | 0.01 μm 15 μm      | Q[1,4.7 <i>d</i> ], ( <i>d</i> in µm) (**)<br>Published CMC<br>uncertainty for a different<br>instrument  |
| NMISA  | Form Talysurf PGI 840  | 1000     | 2   |    | 250 | Diameter<br>standard                                | 0.01 3000 μm       | (4 + 20 <i>d</i> ) ( <i>d</i> in μm)  |
| RISE   | Form Talysurf 120 with inductive pick-up                     | < 0.7 mN | 2   | 90 | 500 | Gauge blocks  | 0.05 μm<br>1000 μm | Q[5,20 <i>d</i> ] ( <i>d</i> in μm)   |
| UME    | Mahr Surf XCR 20 (pick up<br>MFW-250 B)                      | 700      | 2   | 60 | 100 | Depth setting<br>standard<br>calibrated by<br>PTB   | 0.01 μm 50 μm      | No CMC entry available for<br>this instrument.<br>Requested uncertainty:<br>Q[38,3 <i>d</i> ] ( <i>d</i> in μm) (*)<br>Available CMC entry:<br>Q[33,13 <i>d</i> ] ( <i>d</i> in μm) |
| VNIIMS | Form Talysurf PGI 420  | 70       | 2   |    | 250 | reference<br>sphere                                 | 1 μm 3 μm          | Q[1.6,0.007 <i>d</i> ] ( <i>d</i> in nm)  |

| VTT | Bruker GT-K optical 3D<br>profiler (coherence scanning<br>interferometer) | objective<br>2.5 x and<br>0.55x<br>secondary<br>lens | pixel size<br>7.5 μm |  | Gauge blocks | No CMC entry available<br>for this instrument.<br>Requested uncertainty:<br>Q[23.4, 35.6 <i>d</i> ] ( <i>d</i> in μm)<br>(*) |
|-----|---|--|----------------------|--|--------------|--|
|     |   |  |                      |  |              |  |

Q[a,b] is the quadrature sum of a & b, and *d* is the groove depth.

(\*) CMCs that are not official at the present moment because they are still in process

(\*\*) CMCs that correspond to a different declared technique

## 10 Appendix B All measurements performed

The pilot laboratory carried out the first and last measurement of the standards and at the end of the comparison measurements also carried out a control measurement with its traceable reference stylus instrument HRTS [11] which has a vertical measurement range of 450  $\mu$ m. Thus, the two deepest grooves could not be measured.

The list of measured values also contains the first measurement of the VTT (VTT 1st) before cleaning the standard EN19\_7.

**Table 12.** 900  $\mu$ m groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean.

| 900 µm     | Xi      | u(x <sub>i</sub> ) | U(x <sub>i</sub> ) | En   | $(x_i - \bar{x}_w)$ | $U(x_i - \bar{x}_w)$ | Contribu- |
|------------|---------|--------------------|--------------------|------|---------------------|----------------------|-----------|
|            |         |                    |                    |      |                     |                      | tion to   |
|            | μm      | μm                 | μm                 |      | μm                  | μm                   | ref. val. |
| PTB        | 899.884 | 0.027              | 0.054              | 0.42 | -0.020              | 0.048                | Y         |
| VNIIMS     | 899.825 | 0.049              | 0.098              | 0.84 | -0.079              | 0.095                | Y         |
| NMISA      | 899.907 | 0.049              | 0.097              | 0.03 | 0.003               | 0.094                | Y         |
| UME        | 900.156 | 0.061              | 0.123              | 2.01 | 0.252               | 0.125                | Ν         |
| RISE       | 899.650 | 4.160              | 8.320              | 0.03 | -0.254              | 8.320                | Y         |
| VTT 1st    | 899.861 | 0.040              | 0.080              | 0.52 | -0.043              | 0.084                | Ν         |
| BEV        | 899.919 | 0.016              | 0.032              | 0.76 | 0.015               | 0.019                | Y         |
| INRIM      | 899.960 | 0.210              | 0.420              | 0.13 | 0.056               | 0.419                | Y         |
| GUM        | 900.504 | 0.527              | 1.054              | 0.57 | 0.600               | 1.054                | Y         |
| CEM        | *       | *                  | *                  | *    | *                   | *                    | *         |
| VTT 2nd    | 899.870 | 0.130              | 0.260              | 0.13 | -0.034              | 0.259                | Y         |
| PTB end    | 899.896 | 0.027              | 0.054              | 0.14 | -0.008              | 0.060                | Ν         |
| Mean value | 899.940 |                    |                    |      |                     |                      |           |

Stand. dev. 0.231 Ref. value **899.904** 

Uncertainty 0.025

**Table 13.** 600  $\mu$ m groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean.

| 600 μm      | Xi      | <i>u</i> ( <i>x</i> <sub>i</sub> ) | $U(x_i)$ | En    | $(x_i - \bar{x}_w)$ | $U(x_i -$     | Contribu- |
|-------------|---------|------------------------------------|----------|-------|---------------------|---------------|-----------|
|             |         |                                    |          |       |                     | $\bar{x}_w$ ) | tion to   |
|             | μm      | μm                                 | μm       |       | μm                  | μm            | ref. val. |
| РТВ         | 599.913 | 0.022                              | 0.044    | 0.12  | -0.004              | 0.037         | Y         |
| VNIIMS      | 599.893 | 0.045                              | 0.090    | 0.28  | -0.024              | 0.087         | Y         |
| NMISA       | 599.931 | 0.044                              | 0.088    | 0.16  | 0.014               | 0.085         | Y         |
| UME         | 601.287 | 0.052                              | 0.104    | 12.82 | 1.370               | 0.107         | Ν         |
| RISE        | 599.810 | 2.770                              | 5.540    | 0.02  | -0.107              | 5.540         | Y         |
| VTT 1st     | 599.914 | 0.032                              | 0.064    | 0.05  | -0.003              | 0.068         | Ν         |
| BEV         | 599.921 | 0.016                              | 0.032    | 0.17  | 0.004               | 0.022         | Y         |
| INRIM       | 599.960 | 0.160                              | 0.320    | 0.13  | 0.043               | 0.319         | Y         |
| GUM         | 599.437 | 0.351                              | 0.702    | 0.68  | -0.480              | 0.702         | Y         |
| CEM         | *       | *                                  | *        | *     | *                   | *             | *         |
| VTT 2nd     | 599.934 | 0.087                              | 0.174    | 0.10  | 0.017               | 0.172         | Y         |
| PTB end     | 599.927 | 0.023                              | 0.045    | 0.19  | 0.01                | 0.051         | Ν         |
| Mean value  | 599.850 |                                    |          |       |                     |               |           |
| Stand. dev. | 0.162   |                                    |          |       |                     |               |           |
| Ref. value  | 599.917 |                                    |          |       |                     |               |           |
| Uncertainty | 0.024   |                                    |          |       |                     |               |           |

**Table 14.** 200 µm groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean.

| 200 µm      | Xi      | <i>u</i> ( <i>x</i> <sub>i</sub> ) | U(x <sub>i</sub> ) | En    | $(x_i - \bar{x}_w)$ | $U(x_i - \bar{x}_w)$ | Contribu-            |
|-------------|---------|------------------------------------|--------------------|-------|---------------------|----------------------|----------------------|
|             | μm      | μm                                 | μm                 |       | μm                  | μm                   | tion to<br>ref. val. |
| РТВ         | 199.989 | 0.015                              | 0.029              | 0.78  | 0.019               | 0.024                | Y                    |
| VNIIMS      | 199.956 | 0.039                              | 0.078              | 0.19  | -0.014              | 0.076                | Y                    |
| NMISA       | 199.971 | 0.038                              | 0.076              | 0.01  | 0.001               | 0.074                | Y                    |
| UME         | 201.039 | 0.034                              | 0.067              | 15.50 | 1.069               | 0.069                | Ν                    |
| RISE        | 199.970 | 0.920                              | 1.840              | 0.00  | 0.000               | 1.840                | Y                    |
| VTT 1st     | 200.032 | 0.024                              | 0.048              | 1.23  | 0.062               | 0.051                | Ν                    |
| BEV         | 199.965 | 0.016                              | 0.032              | 0.18  | -0.005              | 0.028                | Y                    |
| INRIM       | 199.910 | 0.080                              | 0.160              | 0.38  | -0.060              | 0.159                | Y                    |
| GUM         | 199.949 | 0.127                              | 0.254              | 0.08  | -0.021              | 0.253                | Y                    |
| CEM         | 199.965 | 0.016                              | 0.032              | 0.19  | -0.005              | 0.028                | Y                    |
| VTT 2nd     | 199.945 | 0.029                              | 0.058              | 0.45  | -0.025              | 0.056                | Y                    |
| PTB end     | 199.977 | 0.015                              | 0.029              | 0.20  | 0.007               | 0.033                | Ν                    |
| PTB HRTS    | 199.947 | 0.008                              | 0.016              | 0.83  | -0.023              | 0.028                | Ν                    |
| Mean value  | 199.958 |                                    |                    |       |                     |                      |                      |
| Stand. dev. | 0.021   |                                    |                    |       |                     |                      |                      |
| Ref. value  | 199.970 |                                    |                    |       |                     |                      |                      |
| Uncertainty | 0.016   |                                    |                    |       |                     |                      |                      |

**Table 15.** 50 µm groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean.

| 50 µm       | Xi       | u(x <sub>i</sub> ) | U(x <sub>i</sub> ) | En   | $(x_i - \bar{x}_w)$ | $U(x_i-\bar{x}_w)$ | Contribu- |
|-------------|----------|--------------------|--------------------|------|---------------------|--------------------|-----------|
|             | um       | uт                 | um                 |      | uт                  | um                 | tion to   |
|             | <b>F</b> | P                  | P****              |      | P****               | <b>P</b>           | mean      |
| РТВ         | 50.274   | 0.013              | 0.026              | 0.24 | 0.005               | 0.022              | Y         |
| VNIIMS      | 50.269   | 0.037              | 0.074              | 0.00 | 0.000               | 0.073              | Y         |
| NMISA       | 50.266   | 0.044              | 0.087              | 0.03 | -0.003              | 0.086              | Y         |
| UME         | 50.245   | 0.024              | 0.048              | 0.53 | -0.024              | 0.046              | Y         |
| RISE        | 50.273   | 0.233              | 0.466              | 0.01 | 0.004               | 0.466              | Y         |
| VTT 1st     | 50.353   | 0.023              | 0.046              | 1.74 | 0.084               | 0.048              | Ν         |
| BEV         | 50.270   | 0.026              | 0.052              | 0.02 | 0.001               | 0.050              | Y         |
| INRIM       | 50.240   | 0.070              | 0.140              | 0.21 | -0.029              | 0.139              | Y         |
| GUM         | 50.220   | 0.034              | 0.068              | 0.74 | -0.049              | 0.066              | Y         |
| CEM         | 50.277   | 0.012              | 0.023              | 0.45 | 0.008               | 0.018              | Y         |
| VTT 2nd     | 50.351   | 0.008              | 0.016              | 3.81 | 0.082               | 0.022              | Ν         |
| PTB end     | 50.279   | 0.012              | 0.024              | 0.36 | 0.010               | 0.028              | Ν         |
| PTB HRTS    | 50.284   | 0.004              | 0.009              | 0.89 | 0.015               | 0.017              | Ν         |
| Mean value  | 50.259   |                    |                    |      |                     |                    |           |
| Stand. dev. | 0.019    |                    |                    |      |                     |                    |           |
| Ref. value  | 50.269   |                    |                    |      |                     |                    |           |
| Uncertainty | 0.015    |                    |                    |      |                     |                    |           |

**Table 16.** 20  $\mu$ m groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean.

| 20 µm       | Xi     | <i>u</i> ( <i>x</i> <sub>i</sub> ) | U(x <sub>i</sub> ) | En   | $(x_i - \bar{x}_w)$ | $U(x_i-\bar{x}_w)$ | Xi |
|-------------|--------|------------------------------------|--------------------|------|---------------------|--------------------|----|
|             | μm     | μm                                 | μm                 |      | μm                  | μm                 |    |
| РТВ         | 21.900 | 0.012                              | 0.023              | 0.21 | 0.005               | 0.022              | Y  |
| VNIIMS      | 21.896 | 0.037                              | 0.074              | 0.01 | 0.001               | 0.073              | Y  |
| NMISA       | 21.897 | 0.036                              | 0.071              | 0.02 | 0.002               | 0.071              | Y  |
| UME         | 21.886 | 0.024                              | 0.049              | 0.20 | -0.010              | 0.048              | Y  |
| RISE        | 21.882 | 0.103                              | 0.206              | 0.06 | -0.013              | 0.206              | Y  |
| VTT 1st     | 21.945 | 0.023                              | 0.046              | 1.07 | 0.050               | 0.046              | Ν  |
| BEV         | 21.896 | 0.004                              | 0.009              | 0.11 | 0.001               | 0.006              | Y  |
| INRIM       | 21.880 | 0.070                              | 0.140              | 0.11 | -0.015              | 0.140              | Y  |
| GUM         | 21.873 | 0.017                              | 0.034              | 0.67 | -0.022              | 0.033              | Y  |
| CEM         | 21.896 | 0.005                              | 0.011              | 0.09 | 0.001               | 0.009              | Y  |
| VTT 2nd     | 21.948 | 0.005                              | 0.009              | 4.82 | 0.053               | 0.011              | Ν  |
| PTB end     | 21.902 | 0.012                              | 0.023              | 0.28 | 0.007               | 0.024              | Ν  |
| PTB HRTS    | 21.900 | 0.004                              | 0.007              | 0.50 | 0.005               | 0.009              | Ν  |
| Mean value  | 21.890 |                                    |                    |      |                     |                    |    |
| Stand. dev. | 0.009  |                                    |                    |      |                     |                    |    |
| Ref. value  | 21.895 |                                    |                    |      |                     |                    |    |
| Uncertainty | 0.006  |                                    |                    |      |                     |                    |    |

**Table 17.** 5 µm groove: Measurement values, standard and expanded uncertainties,  $E_n$  values, degrees of equivalence  $x_i - \bar{x}_w$ , associated expanded uncertainties  $U(x_i - \bar{x}_w)$  and contribution to the weighted mean.

| 5 μm        | Xi    | <i>u</i> ( <i>x</i> <sub>i</sub> ) | U(x <sub>i</sub> ) | En   | $(x_i - \bar{x}_w)$ | $U(x_i-\bar{x}_w)$ | Contribu-       |
|-------------|-------|------------------------------------|--------------------|------|---------------------|--------------------|-----------------|
|             | μm    | μm                                 | μm                 |      | μm                  | μm                 | tion to<br>mean |
| РТВ         | 5.050 | 0.011                              | 0.022              | 0.04 | -0.001              | 0.021              | Y               |
| VNIIMS      | 5.035 | 0.037                              | 0.073              | 0.22 | -0.016              | 0.073              | Y               |
| NMISA       | 5.047 | 0.036                              | 0.071              | 0.05 | -0.004              | 0.071              | Y               |
| UME         | 5.054 | 0.021                              | 0.041              | 0.06 | 0.003               | 0.041              | Y               |
| RISE        | 5.045 | 0.029                              | 0.058              | 0.10 | -0.006              | 0.058              | Y               |
| VTT 1st     | 5.064 | 0.023                              | 0.046              | 0.28 | 0.013               | 0.046              | Ν               |
| BEV         | 5.051 | 0.005                              | 0.011              | 0.02 | 0.000               | 0.009              | Y               |
| INRIM       | 5.120 | 0.050                              | 0.100              | 0.69 | 0.069               | 0.100              | Y               |
| GUM         | 5.049 | 0.017                              | 0.034              | 0.06 | -0.002              | 0.033              | Y               |
| CEM         | 5.051 | 0.005                              | 0.009              | 0.02 | 0.000               | 0.007              | Y               |
| VTT 2       | 5.062 | 0.004                              | 0.007              | 1.16 | 0.011               | 0.010              | Ν               |
| PTB end     | 5.070 | 0.011                              | 0.022              | 0.84 | 0.019               | 0.023              | Ν               |
| PTB HRTS    | 5.046 | 0.003                              | 0.006              | 0.55 | -0.005              | 0.009              | Ν               |
| Mean value  | 5.056 |                                    |                    |      |                     |                    |                 |
| Stand. dev. | 0.023 |                                    |                    |      |                     |                    |                 |
| Ref. value  | 5.051 |                                    |                    |      |                     |                    |                 |
| Uncertainty | 0.006 |                                    |                    |      |                     |                    |                 |

### 11 Appendix C Measuring uncertainties of the participants

Most of the participants submitted results supported by a full uncertainty calculation. Some partners submitted two uncertainty budgets, one for the three silicon standards (50/20/5  $\mu$ m) and a separate one for the three deeper grooves (900/600/200  $\mu$ m). The following abbreviations are used for the different uncertainty distributions:

N = normal; R = rectangular; T = triangular; U = U-shaped.

#### 11.1 PTB

| Quantity<br>X <sub>i</sub>   | Estimate<br><i>X</i> i | Uncertainty<br>u(x <sub>i</sub> ) | Probability distribution | Sensitivity<br>coefficient<br><i>c</i> i | Uncertainty<br>contribution<br><i>u</i> <sub>i</sub> ( <i>d</i> ) | Degrees of<br>freedom<br><i>v</i> i |
|------------------------------|------------------------|-----------------------------------|--------------------------|--|---|-------------------------------------|
| Scattering                   | 0                      | 10.9 nm                           | N                        | 1  | 3.6 nm  | 8                                   |
| Flatness feed unit,<br>drift | 0                      | 10.5 nm                           | R                        | 1  | 6.1 nm  | ~                                   |
| Form deviation               | 0                      | 10 nm                             | R                        | 1  | 5.8 nm  | 8                                   |

Table 18 Exemplary standard uncertainty budget for PTB measurements

| Reproducibility<br>calibration Instrument | 899.884 | 4.2E-6   | Ν | 1        | 3.8 nm | 5    |
|---|---------|----------|---|----------|--------|------|
| Reference standard                        | 0       | 10 nm    | Ν | 1        | 10 nm  | ~    |
| Gradient groove depth in y-direction      | 0       | ± 0.2 mm | R | 10 nm/mm | 2.0 nm | 8    |
| Noise                                     | 0       | 2.0 nm   | R | 1        | 1.2 nm | ~    |
| Thermal expansion                         | 0       | 1.73     | R | 1        | 1.0 nm | 8    |
|   |         |          |   |          | 27 nm  | 1925 |

#### 11.2 BEV

Table 19 BEV standard uncertainty budget for the groove depths 900/600/200  $\mu m$ 

| Quantity<br><i>X</i> i | estimate<br><i>x</i> i | uncertainty<br><i>u</i> (x <sub>i</sub> ) | probability<br>distribution | sensitivity<br>coefficient<br>c <sub>i</sub> | uncertainty<br>contribution<br>u <sub>i</sub> (d) | degrees of<br>freedom<br>v <sub>i</sub> |
|------------------------|------------------------|---|-----------------------------|--|---|---|
| N1                     | 0                      | 1 nm                                      | N                           | 1  | 0.0010 μm   | 8                                       |
| <b>N</b> 2             | 0                      | 0.1 nm                                    | R                           | 1  | 0.0001 µm   | ~                                       |
| <b>N</b> 3             | 0                      | 0.2 nm                                    | R                           | 1  | 0.0001 µm   | ~                                       |
| <b>N</b> 4             | 0                      | 4 nm                                      | R                           | 1  | 0.0023 μm   | 8                                       |
| <i>P</i> <sub>1</sub>  | 0                      | ±5 μm per<br>edge                         | R                           | 0.00004                                      | 0.0002 μm   | ∞                                       |
| P <sub>2</sub>         | 0                      | ±100 μm                                   | R                           | 2 nm/mm                                      | 0.0002 μm   | 8                                       |
| <i>P</i> <sub>3</sub>  | 0                      | 15 nm                                     | N                           | 1  | 0.0150 µm   | 8                                       |
| P4                     | 0                      | 10 % of<br>correction                     | Ν                           | 1  | 0.0007 μm<br>0.0019 μm<br>0.0033 μm               | ×                                       |
| <i>S</i> <sub>1</sub>  | 0                      | 0.0008 μm<br>0.0027 μm<br>0.0035 μm       | Х                           | 1  | 0.0008 μm<br>0.0027 μm<br>0.0035 μm               | ∞                                       |

 $N_1$ : z-laser interferometer, traceability

 $N_2$ : z-laser interferometer, influence of interpolation error on fit value

 $N_3$ : z-laser interferometer, influence of resolution on fit value

 $N_4$ : z-reference mirror form deviations, influence on fit value

 $P_1$ : Contribution due to feature edge localization in scan direction taking into account sample form deviation

 $P_2$ : Contribution due to profile localization normal to scan direction taking into account sample form deviation

P<sub>3</sub>: Inequality of optical surface properties between groove and top (contamination, etc. )

*P*<sub>4</sub>: Thermal expansion effects

 $S_1$ : "Scatter"  $\sigma_{n-1}$  as defined in protocol

| Table 20 BEV standard uncertainty budget for the groove dep | ths 50/20/5 μm |
|---|----------------|
|---|----------------|

| Quantity<br><i>X</i> i | estimate<br><i>x</i> i | uncertainty<br>u(x <sub>i</sub> ) | probability<br>distribution | sensitivity<br>coefficient | uncertainty contribution | degrees of<br>freedom |
|------------------------|------------------------|-----------------------------------|-----------------------------|----------------------------|--------------------------|-----------------------|
|                        |                        |                                   |                             | Ci                         | u <sub>i</sub> (d)       | Vi                    |
| N <sub>1</sub>         | 0                      | 0.1 nm                            | N                           | 1                          | 0.0001 μm                | 8                     |
| N2                     | 0                      | 0.1 nm                            | R                           | 1                          | 0.0001 μm                | 8                     |

| <b>N</b> 3            | 0 | 0.2 nm     | R | 1        | 0.0001 μm | ~ |
|-----------------------|---|------------|---|----------|-----------|---|
| <b>N</b> 4            | 0 | 4 nm       | R | 1        | 0.0023 μm | 8 |
| <i>P</i> <sub>1</sub> | 0 | ±5 μm per  | R | -        | 0.0002 μm | 8 |
|                       |   | edge       |   |          |           |   |
| P <sub>2</sub>        | 0 | ±5 μm      | R | 58 nm/mm | 0.0002 μm | 8 |
| <i>P</i> <sub>3</sub> | 0 | 3 nm       | N | 1        | 0.0003 μm | 8 |
| <b>P</b> <sub>4</sub> | 0 | 10 % of    | N | 1        | 0.0005 μm | 8 |
|                       |   | correction |   |          |           |   |
| <i>S</i> <sub>1</sub> | 0 | 0.0047 μm  | Х | 1        | 0.0047 μm | 8 |
|                       |   | 0.0037 μm  |   |          | 0.0037 μm |   |
|                       |   | 0.0260 µm  |   |          | 0.0260 µm |   |

#### 11.3 CEM

Table 21 CEM standard uncertainty budget for the groove depths 900/600/200  $\mu m$ 

| Quantity               | estimate                | Uncertainty            | probability  | sensitivity | uncertainty        | degrees of |
|------------------------|-------------------------|------------------------|--------------|-------------|--------------------|------------|
| Xi                     | <b>X</b> i              | u(x <sub>i</sub> )     | distribution | coefficient | contribution       | freedom    |
|                        |                         |                        |              | Ci          | u <sub>i</sub> (d) | Vi         |
| d <sub>ref20</sub>     | 199971.3 nm             | 9                      | N            | 0.99997     | 8.999734           | 60         |
| d <sub>refm20</sub>    | 199341.365 nm           | 2.681 nm               | N            | 1.00313     | 2.689839           | 109        |
| inhomogenity           |                         | 2.676 nm               |              | 0.999973    |                    | 109        |
| σ (dpm)                | 2.889 nm                | 0.463 nm               | N            |             |                    | 38         |
| max-min(Avi)           | 4.537 nm                | 2.619 nm               | R            |             |                    | 100        |
| resolution             | 1.000 nm                | 0.289 nm               | R            |             |                    | 100        |
| Expans. coeff.         | 16.6E-6 K <sup>-1</sup> | 0.5E-6 K <sup>-1</sup> | R            | 318937.767  |                    | 60         |
| α                      |                         |                        |              |             |                    |            |
| Т                      |                         | 0.024 K                |              | 3.308979    |                    | 118        |
| thermometer            |                         |                        |              |             |                    |            |
| calibration            | 0.005 K                 | 0.003 K                | N            |             |                    | 60         |
| drift                  | 0.01 K                  | 0.006 K                | R            |             |                    | 100        |
| resolution             | 0.01 K                  | 0.003 K                | R            |             |                    | 100        |
| ΔΤ                     | 0.08 K                  | 0.023 K                | R            |             |                    | 100        |
| C1(noise)              | 0 nm                    | 0.82272 nm             | R            | 1           | 0.82272            | 100        |
| C2(T)                  | 0 nm                    | 0.32472 nm             | R            | 1           | 0.32472            | 100        |
| <b>d</b> <sub>20</sub> | 199335.482nm            | 12.6921nm              | N            | 1.003160    | 12.73357           | 112        |
| inhomogenity           |                         | 12.69205 nm            |              | 0.999970    |                    | 113        |
| σ (dpm)                | 8.031 nm                | 2.677 nm               | Ν            |             |                    | 8          |
| max-min(Avi)           | 3.591                   | 2.073 nm               | R            |             |                    | 100        |
| resolution             | 1.000 nm                | 0.289 nm               | R            |             |                    | 100        |
| small sample           | 21.181 nm               | 12.229 nm              | R            |             |                    | 100        |
| Expans. coeff.         | 16.6E-6 K <sup>-1</sup> | 0.5E-6 K <sup>-1</sup> | R            | 354806.675  |                    | 60         |
| Т                      |                         | 0.035 K                |              | 3.308969    |                    | 108        |
| thermometer            |                         |                        |              |             |                    |            |
| calibration            | 0.005 K                 | 0.003 K                | N            |             |                    | 60         |
| drift                  | 0.01 K                  | 0.006 K                | R            |             |                    | 100        |
| resolution             | 0.01 K                  | 0.003 K                | R            |             |                    | 100        |
| ΔΤ                     | 0.12 K                  | 0.035 K                | R            |             |                    | 100        |
| rounded                | 0.399 nm                |                        |              |             |                    |            |

*d* = 199965,399 nm

uc (*d*) = 16.2 nm

 $v_{eff}$  = 202

| Quantity                        | estimate                | Uncertainty            | probability  | sensitivity             | uncertainty        | degrees of             |
|---------------------------------|-------------------------|------------------------|--------------|-------------------------|--------------------|------------------------|
| Xi                              | Xi                      | u(x <sub>i</sub> )     | distribution | coefficient             | contribution       | freedom                |
|                                 |                         |                        |              | Ci                      | u <sub>i</sub> (d) | Vi                     |
| d <sub>ref20</sub>              | 5052 nm                 | 3                      | N            | 0.999 715               | 2.999 14           | 60                     |
| d <sub>refm20</sub>             | 5051.079 nm             | 0.427 26 nm            | N            | 0.999 897               | 0.427 21           | 233                    |
| inhomogenity                    |                         | 0.427 236 nm           |              | 0.999 995               |                    | 234                    |
| $\sigma$ (d <sub>refm20</sub> ) | 1.159 nm                | 0.186 nm               | N            |                         |                    | 38                     |
| max-min(Av <sub>i</sub> )       | 0.441 nm                | 0.254 nm               | R            |                         |                    | 100                    |
| resolution                      | 1.000 nm                | 0.289 nm               | R            |                         |                    | 100                    |
| Expans. coeff.                  | 2.56E-6 K <sup>-1</sup> | 0.5E-6 K <sup>-1</sup> | R            | 9091.8994               |                    | 60                     |
| Т                               |                         | 0.024 K                |              | 0.012 931               |                    | 118                    |
| thermometer                     |                         |                        |              |                         |                    |                        |
| calibration                     | 0.005 K                 | 0.003 K                | N            |                         |                    | 60                     |
| drift                           | 0.01 K                  | 0.006 K                | R            |                         |                    | 100                    |
| resolution                      | 0.01 K                  | 0.003 K                | R            |                         |                    | 100                    |
| ΔΤ                              | 0.08 K                  | 0.023 K                | R            |                         |                    | 100                    |
| C1(noise)                       | 0 nm                    | 0.9295 nm              | R            | 1                       | 0.929 534          | 100                    |
| C2(T)                           | 0 nm                    | 0.001 115 nm           | R            | 1                       | 0.001 115          | 100                    |
| <b>d</b> <sub>20</sub>          | 5049.636 nm             | 2.5585 nm              | N            | 1,000 182               | 2.558 997          | 71                     |
| inhomogenity                    |                         | 2.558 53 nm            |              | 0.999 995               |                    | 72                     |
| σ (dpm)                         | 4.158 nm                | 1.386 nm               | N            |                         |                    | 8                      |
| max-min(Avi)                    | 1.750 nm                | 1.010 nm               | R            |                         |                    | 100                    |
| resolution                      | 1.000 nm                | 0.289 nm               | R            |                         |                    | 100                    |
| small sample                    | 3.250 nm                | 1.876 nm               | R            |                         |                    | 100                    |
| Expans. coeff.                  | 2.56E-6 K <sup>-1</sup> | 0.5E-6 K <sup>-1</sup> | R            | 10 099.221              |                    | 60                     |
| Т                               |                         | 0.019 K                |              | 0.012 927               |                    | 133                    |
| thermometer                     |                         |                        |              |                         |                    |                        |
| calibration                     | 0.005 K                 | 0.003 K                | N            |                         |                    | 60                     |
| drift                           | 0.01 K                  | 0.006 K                | R            |                         |                    | 100                    |
| resolution                      | 0.01 K                  | 0.003 K                | R            |                         |                    | 100                    |
| ΔΤ                              | 0.06 K                  | 0.017 K                | R            |                         |                    | 100                    |
| rounded                         | 0.442 nm                |                        |              |                         |                    |                        |
|                                 |                         | <i>d</i> = 5050,6 nm   |              | uc ( <i>d</i> ) = 4.5 n | m                  | v <sub>eff</sub> = 212 |

Table 22 CEM standard uncertainty budget for the groove depths 50/20/5  $\mu m$ 

#### 11.4 GUM

| Quantity       | Estimate  | Uncertainty                       | Probability  | Sensitivity | Uncertainty                        | Degrees of |
|----------------|-----------|-----------------------------------|--------------|-------------|------------------------------------|------------|
| Xi             | Xi        | u(x <sub>i</sub> )                | distribution | coefficient | contribution                       | freedom    |
|                |           |                                   |              | Ci          | <i>u</i> <sub>i</sub> ( <i>d</i> ) | Vi         |
| Dn             | 75,308 μm | 12.5 nm                           | N            | 1           | 12.5 nm                            | 100        |
| ∆Pt            | 0 nm      | 0.33 nm                           | R            | 1           | 0.33 nm                            | 8          |
| b              | 0 nm      | sr(Ptm)                           | N            | 1           | sr(Ptm)                            | 100        |
| Zt             | 0 nm      | s <sub>t</sub> (Pt <sub>m</sub> ) | N            | 1           | s <sub>t</sub> (Pt <sub>m</sub> )  | 100        |
| Zref           | 0 nm      | 4.18 nm                           | R            | 1           | 4.18 nm                            | 8          |
| Z <sub>0</sub> | 0 nm      | 10.45 nm                          | R            | 1           | 10.45 nm                           | 8          |
| A              | 0 nm      | 1.44 nm                           | R            | 1           | 1.44 nm                            | 8          |

| Quantity | estimate  | uncertainty                       | probability  | sensitivity | uncertainty                       | degrees of |
|----------|-----------|-----------------------------------|--------------|-------------|-----------------------------------|------------|
| Xi       | Xi        | u(x <sub>i</sub> )                | distribution | coefficient | contribution                      | freedom    |
|          |           |                                   |              | Ci          | u <sub>i</sub> (d)                | Vi         |
| Dn       | 24.003 μm | 11.5 nm                           | N            | 1           | 11.5                              | 100        |
| ΔPt      | 0 nm      | 0.33 nm                           | R            | 1           | 0.33 nm                           | 8          |
| b        | 0 nm      | sr(Ptm)                           | N            | 1           | sr(Ptm)                           | 100        |
| Zt       | 0 nm      | s <sub>t</sub> (Pt <sub>m</sub> ) | N            | 1           | s <sub>t</sub> (Pt <sub>m</sub> ) | 100        |
| Zref     | 0 nm      | 4.18 nm                           | R            | 1           | 4.18 nm                           | 8          |
| Zo       | 0 nm      | 10.45 nm                          | R            | 1           | 10.45 nm                          | 8          |
| A        | 0 nm      | 1.44 nm                           | R            | 1           | 1.44 nm                           | 8          |

Table 24 GUM standard uncertainty budget for the groove depths 50/20/5  $\mu m$ 

Used symbols:

D<sub>n</sub> - Reference standard depth

 $\Delta Pt$  - Transfer of Pt from reference standard

b - repeatability of reference standard measurement

 $z_{t}\xspace$  - heterogenity of measured standard

z<sub>ref</sub> - nonlinearity of measuring station

 $\boldsymbol{z}_0$  - noise of measuring station

A - tilt of measured standard

#### **11.5 INRIM**

Table 25 INRIM standard uncertainty budget for the groove depth 900  $\mu m$ 

|                               | EN10 7                             |                 | ano orro dom | 44 000   |            |   |                                       |  |
|-------------------------------|------------------------------------|-----------------|--------------|----------|------------|---|---------------------------------------|--|
|                               | EN19_/ nominal groove depth 900 µm |                 |              |          |            |   |                                       |  |
| Quantity (x <sub>i</sub> )    | $u(x_i)$                           | unit            | $u(x_i)/x_i$ | distrib. | <i>v</i> i | $c_{\rm i} = \delta f / \delta x_{\rm i}$ | <i>u</i> <sub>i</sub> ( <i>y</i> )/nm |  |
| Repeatability                 | 2,9                                | nm              |              | N        | 8          | 1   | 3                                     |  |
|                               |                                    |                 |              |          |            |   |                                       |  |
| z-axis calibration            |                                    |                 | 2,2E-04      | N        | 10         | 900060                                    | 198                                   |  |
|                               |                                    |                 |              |          |            |   |                                       |  |
| Probe readings                |                                    |                 |              |          |            |   |                                       |  |
| digital resolution 16 bit ADC | 10                                 | nm              |              | R        | 100        | 0,58                                      | 6                                     |  |
| profile noise                 | 50                                 | nm              |              | R        | 50         | 0,58                                      | 29                                    |  |
|                               |                                    |                 |              |          |            |   |                                       |  |
| straightness (x-axis)         | 50                                 | nm              |              | R        | 50         | 0,58                                      | 29                                    |  |
| levelling                     |                                    |                 | 5E-05        | N        | 50         | 900060                                    | 45                                    |  |
|                               |                                    |                 |              |          |            |   |                                       |  |
| Thermal effects               | 1,7E-05                            | K <sup>-1</sup> |              | N        | 50         | 450030                                    | 7                                     |  |
| CTE 16,6*10 <sup>-6</sup> /°C |                                    |                 |              |          |            |   |                                       |  |

| Combined standard uncertainty | 208  | nm |
|-------------------------------|------|----|
| ν <sub>eff</sub>              | 12   |    |
| k                             | 2,18 |    |
| Expanded uncertainty          | 452  | nm |

|                               | SN 497 nominal groove depth 5 μm |      |              |          |                |                               |                        |  |  |  |  |  |  |
|-------------------------------|----------------------------------|------|--------------|----------|----------------|-------------------------------|------------------------|--|--|--|--|--|--|
| Quantity (x <sub>i</sub> )    | $u(x_i)$                         | unit | $u(x_i)/x_i$ | distrib. | ν <sub>i</sub> | $c_i = \delta f / \delta x_i$ | u <sub>i</sub> (y) /nm |  |  |  |  |  |  |
| Repeatability                 | 4,5                              | nm   |              | N        | 8              | 1                             | 4                      |  |  |  |  |  |  |
|                               |                                  |      |              |          |                |                               |                        |  |  |  |  |  |  |
| z-axis calibration            |                                  |      | 5E-03        | N        | 10             | 5121                          | 26                     |  |  |  |  |  |  |
|                               |                                  |      |              |          |                |                               |                        |  |  |  |  |  |  |
| Probe readings                |                                  |      |              |          |                |                               |                        |  |  |  |  |  |  |
| digital resolution 16 bit ADC | 10                               | nm   |              | R        | 100            | 0,58                          | 6                      |  |  |  |  |  |  |
| profile noise                 | 50                               | nm   |              | R        | 50             | 0,58                          | 29                     |  |  |  |  |  |  |
|                               |                                  |      |              |          |                |                               |                        |  |  |  |  |  |  |
| straightness (x-axis)         | 50                               | nm   |              | R        | 50             | 0,58                          | 29                     |  |  |  |  |  |  |
| levelling                     |                                  |      | 1E-04        | N        | 50             | 5121                          | 1                      |  |  |  |  |  |  |

#### Table 26 INRIM standard uncertainty budget for the groove depth 5 $\mu\text{m}$

| combined standard uncertainty | 49 | nm |
|-------------------------------|----|----|
| $v_{eff}$                     | 80 |    |
| k                             | 2  |    |
| Expanded uncertainty          | 98 | nm |

#### 11.6 NMISA

Standard uncertainty budget for all grove depths

| Quantity<br><i>X</i> i                               | Estim<br>ate<br><i>x</i> i | Uncertainty<br><i>u</i> (x <sub>i</sub> ) nm             | Pro<br>bab<br>ility<br>dist<br>ribu<br>tion | Sensitivity<br>coefficient<br>c <sub>i</sub> | Uncertainty<br>contribution<br>u <sub>i</sub> (d) | Degrees<br>freedom<br>v <sub>i</sub> | of |
|--|----------------------------|--|---|--|---|--------------------------------------|----|
| Machine<br>specification                             | 0                          | (70 + 30 <i>d</i> [mm])                                  | N   | 1  |   | ~~~~                                 |    |
| Repeatability  | 0                          | $\sigma_r = \sqrt{\frac{\sum_{i=1}^n (x - \bar{x})}{n}}$ | N   | 1  |   | 8                                    |    |
| Total standard<br>uncertainty (all<br>groove depths) |                            | √((70 + )  | 30d) <sup>2</sup>                           | $(2 + \sigma_r^2)$                           |   |                                      |    |

The machine specifications take into account:

- temperature of the machine
- linearity of the probe
- resolution
- software fitting errors

## 11.7 RISE

| Quantity<br>X <sub>i</sub>        | estimate<br><i>X</i> i (nm) | uncertainty<br>u(x <sub>i</sub> ) (nm) | probability<br>distribution | sensitivity<br>coefficient<br><sub>Ci</sub> | uncertainty<br>contribution<br>u <sub>i</sub> (d) (nm) | degrees<br>of<br>freedom<br><i>v</i> i |
|-----------------------------------|-----------------------------|--|-----------------------------|---|--|--|
| Amplification (±0.8%)             | 0.8                         | 0.462                                  | R                           | d   | 0.462 <i>d</i>   | 100                                    |
| Surface variation<br>(topography) | 32.0                        | 20.2                                   | Ν                           | 0.632                                       | 20.2   | 26                                     |
| Guideway profile (Wt)             | 14.0                        | 8.1                                    | R                           | 1   | 8.1  | 1000                                   |
| Noise                             | 3.0                         | 3.0                                    | N                           | 1   | 3.0  | 50                                     |
| Contact deformation               | 2.0                         | 2.0                                    | R                           | 1   | 2.0  | 1000                                   |
| Resolution                        | 15.9                        | 4.6                                    | R                           | 1   | 4.6  | 1E+08                                  |
| Assessment error                  | 15.0                        | 15.0                                   | R                           | 1   | 15.0   | 1000                                   |
| Tip radius                        | 0.0                         | 0.0                                    | R                           | 1   | 0  | 1000                                   |
| Repeatability                     | 2.0                         | 0.9                                    | Ν                           | 1   | 0.9  | 4                                      |
| Temperature contribution          | 1.7                         | 1.7                                    | R                           | 1   | 1.7  | 100                                    |

Table 28 RISE standard uncertainty budget for the groove depths 900/600/200  $\mu m$ 

Table 29 RISE standard uncertainty budget for the groove depths 50/20/5  $\mu m$ 

| quantity<br><i>X</i> i            | estimate | uncertainty<br>u(x <sub>i</sub> ) (nm) | probability<br>distribution | sensitivity<br>coefficient<br><sub>Ci</sub> | uncertainty<br>contribution<br>u <sub>i</sub> (d) (nm) | degrees<br>of<br>freedom<br><i>v</i> i |
|-----------------------------------|----------|--|-----------------------------|---|--|--|
| Amplification (±0.8%)             | 0.8      | 0.462                                  | R                           | d   | 0.462d   | 100                                    |
| Surface variation<br>(topography) | 15.0     | 9.49                                   | N                           | 0.632                                       | 9.5  | 26                                     |
| Guideway profile (Wt)             | 14.0     | 8.1                                    | R                           | 1   | 8.1  | 1000                                   |
| Noise                             | 3.0      | 3.0                                    | N                           | 1   | 3.0  | 50                                     |
| Contact deformation               | 2.0      | 2.0                                    | R                           | 1   | 2.0  | 1000                                   |
| Resolution                        | 0.6      | 0.2                                    | R                           | 1   | 0.2  | 1E+08                                  |
| Assessment error                  | 10.0     | 10.0                                   | R                           | 1   | 10.0   | 1000                                   |
| Tip radius                        | 0        | 0                                      | R                           | 1   | 0  | 1000                                   |
| Repeatability                     | 8.0      | 3.6                                    | N                           | 1   | 3.6  | 4                                      |

#### 11.8 UME

| Table 30 UME | standard uncertaint | y budget for the | groove depths 900 μm |
|--------------|---------------------|------------------|----------------------|
|              |                     | , ,              |                      |

| Uncertainty Sources Input Data Sensitivity Coefficients  |                 |                 |      |                 | nts   | Vari | ances     |            |                 |              |    |          |         |                 |                 |      |       |     |
|--|-----------------|-----------------|------|-----------------|-------|------|-----------|------------|-----------------|--------------|----|----------|---------|-----------------|-----------------|------|-------|-----|
| Explanations   | Symbol          | Estimated Value | Unit | Symbol          | Value | Unit | Prob.Dist | Multiplier | Symbol          | Value        |    | Unit     | Value   |                 | Unit            |      | ui    | vi  |
| Groove depth (U <sub>n</sub> : Uncertainty of Ref.<br>Groove depth standard)   | Dn              | 900016          | nm   | u <sub>Dn</sub> | 114   | nm   | Normal    | 0,5        | C <sub>Dn</sub> | 0,000001     | zu | 1,000156 | 4,0E-09 | zu <sup>2</sup> | nm²             |      | 57,0  | 100 |
| Inaccuracy of measurement location on a<br>groove of the Ref. Groove depth standard  | Ptmy            | 900016          | nm   | Uptmy           | 1     | nm   | Uniform   | 0,5774     | CPtmy           | 0,000001     | zu | 1,000156 | 4,1E-13 | zu <sup>2</sup> | nm²             |      | 0,6   | 100 |
| Reproducebility on the groove of the Ref.<br>Groove depth standard (mt = 15)   | b               | 78              | nm   | u <sub>b</sub>  | 78    | nm   | Normal    | 0,26       | Cb              | 0,000001     | zu | 1,000156 | 5,0E-10 | z,²             | nm²             |      | 20,1  | 14  |
| Dn   | Dn              | 900016          | nm   | UDn             | 114   | nm   | Normal    | 0,5        | CDn             | 0,0000000001 | zu | 1,16E-05 | 5,4E-19 | Zu <sup>2</sup> | nm <sup>2</sup> |      | 0,0   | 100 |
| Linear thermal expansion coefficient of the<br>Ref. Groove depth standard  | $\alpha_{ref}$  | 16,6E-6         | 1/K  | Ua              | 5E-07 | 1/K  | Uniform   | 0,5774     | Ca              | 1            | zu | 630109,2 | 4,1E-14 | z, <sup>2</sup> | nm²             |      | 0,2   | 100 |
| ∆T: (Ref. Groove depth standard's<br>temperature - 20) °C  | ΔT              | 0,7             | °C   | U <sub>ΔT</sub> | 0,3   | °C   | Normal    | 0,5        | $C_{\Delta T}$  | 0,00002      | zu | 14,90658 | 6,2E-12 | zu <sup>2</sup> | nm²             |      | 2,2   | 100 |
| Topography of test standard for 3 different measurement positions ( $m_t = 9$ )  | Dm              | 900156          | nm   | UDm             | 23    | nm   | Normal    | 0,33       | CDm             | 1,00000      |    |          | 58,8    |                 | nm <sup>2</sup> |      | 7,7   | 8   |
| Straightness deviation of the datum of the device (Wt measured on an optical flat)   | Zref            | 20              | nm   | UZref           | 10    | nm   | Uniform   | 0,5774     | CZref           | 1,00000      |    |          | 33      |                 | nm²             |      | 5,8   | 100 |
| Background noise (Rzo measured on an optical flat without $\lambda s$ filter for $\Delta x = 0,0001$ mm, measurement speed V = 0,1 mm/s) | Z <sub>0</sub>  | 18              | nm   | uzo             | 9     | nm   | Uniform   | 0,5774     | Czo             | 0,035355     |    |          | 0,034   |                 | nm²             |      | 0,2   | 100 |
| Uncertainty caused by inexact knowledge of plastic deformation (for metallic standards)  | Z <sub>pl</sub> | 5               | nm   | upl             | 5     | nm   | Uniform   | 0,5774     | C <sub>pl</sub> | 1,00000      |    |          | 8,3     |                 | nm²             |      | 2,9   | 100 |
| Alignment error of the curve fitting (A)   | Ptr             | 20              | nm   | UPly            | 5,0   | nm   | Uniform   | 0,5774     | CPtr            | 1,00000      |    |          | 8       |                 | nm <sup>2</sup> |      | 2,9   | 100 |
| Dm   | Dm              | 900156          | nm   | UDm             | 23    | nm   | Normal    | 0,5        | CDm             | 0,000012     |    |          | 1,8E-08 |                 | nm <sup>2</sup> | 1    | 0,0   | 100 |
| Linear thermal expansion coefficient of the<br>groove depth standard   | $\alpha_{tost}$ | 16,6E-6         | 1/K  | u <sub>a</sub>  | 5E-07 | 1/K  | Uniform   | 0,5774     | Ca              | 630109,2     |    |          | 0,0     |                 | nm²             |      | 0,2   | 100 |
| ΔT: (Test groove depth standard's<br>temperature - 20) °C  | ΔT              | 0,7             | °C   | u <sub>ΔT</sub> | 0,3   | °C   | Normal    | 0,5        | C∆T             | 14,94259     |    |          | 5,0     |                 | nm²             |      | 2,2   | 100 |
| Number of profile points at the top profile sections   | n <sub>h</sub>  | 4000            |      |                 |       |      |           |            |                 |              |    |          |         |                 |                 |      | Total |     |
| Number of profile points at the bottom profile section   | n               | 1000            |      |                 |       |      |           |            |                 |              |    |          |         |                 |                 | Veff | 121   |     |

## TOTAL VARIANCE u<sup>2</sup> = 113,9 + 4,5E-09 D<sup>2</sup> nm<sup>2</sup> Standard Uncertainty u = 61,4 nm

| Uncertainty So   | urces            |                 |      |                 | Ir    | put Dat | a         |            |                   | Sensitivity Coef | ficie | nts              | Vari    | iances          |                 |                |                 |     |
|--|------------------|-----------------|------|-----------------|-------|---------|-----------|------------|-------------------|------------------|-------|------------------|---------|-----------------|-----------------|----------------|-----------------|-----|
| Explanations   | Symbol           | Estimated Value | Unit | Symbol          | Value | Unit    | Prob.Dist | Multiplier | Symbol            | Value            |       | Unit             | Value   |                 | Unit            |                | ui              | vi  |
| Groove depth (U <sub>n</sub> : Uncertainty of Ref.<br>Groove depth standard)   | Dn               | 50009           | nm   | UDn             | 43    | nm      | Normal    | 0,5        | C <sub>Dn</sub>   | 0,000020         | zu    | 1,004711         | 1,8E-07 | zu <sup>2</sup> | nm²             |                | 21,6013         | 100 |
| Inaccuracy of measurement location on a<br>groove of the Ref. Groove depth standard  | Ptmy             | 50009           | nm   | Uptmy           | 1     | nm      | Uniform   | 0,5774     | C <sub>Ptmy</sub> | 0,000020         | zu    | 1,004711         | 1,3E-10 | zu <sup>2</sup> | nm²             |                | 0,5801          | 100 |
| Reproducebility on the groove of the Ref.<br>Groove depth standard (mt = 15)   | b                | 14              | nm   | u <sub>b</sub>  | 14    | nm      | Normal    | 0,26       | C <sub>b</sub>    | 0,000020         | zu    | 1,004711         | 5,2E-09 | zu <sup>2</sup> | nm²             |                | 3,6318          | 14  |
| Dn   | Dn               | 50009           | nm   | UDn             | 43    | nm      | Normal    | 0,5        | CDn               | 0,0000000023     | Zu    | 1,16E-05         | 2,5E-17 | z <sup>2</sup>  | nm <sup>2</sup> | 1 F            | 0,0003          | 100 |
| Linear thermal expansion coefficient of the Ref. Groove depth standard   | $\alpha_{ref}$   | 16,6E-6         | 1/K  | uα              | 5E-07 | 1/K     | Uniform   | 0,5774     | Ca                | 1                | zu    | 35171,22         | 4,1E-14 | zu <sup>2</sup> | nm²             | 1 [            | 0,0102          | 100 |
| ∆T: (Ref. Groove depth standard's temperature - 20) °C   | ΔΤ               | 0,7             | °C   | U <sub>ΔT</sub> | 0,3   | °C      | Normal    | 0,5        | C                 | 0,00002          | zu    | 0,832051         | 6,2E-12 | zu <sup>2</sup> | nm²             |                | 0,1248          | 100 |
| Topography of test standard for 3 different measurement positions ( $m_t = 9$ )  | Dm               | 50244,6         | nm   | u <sub>Dm</sub> | 24,5  | nm      | Normal    | 0,33       | C <sub>Dm</sub>   | 1,00000          |       |                  | 66,7    |                 | nm²             |                | 8,1667          | 8   |
| Straightness deviation of the datum of the device (Wt measured on an optical flat)   | Z <sub>ref</sub> | 20              | nm   | UZref           | 10    | nm      | Uniform   | 0,5774     | CZref             | 1,00000          |       |                  | 33      |                 | nm²             |                | 5,7735          | 100 |
| Background noise (Rzo measured on an optical flat without $\lambda s$ filter for $\Delta x = 0,0001$ mm, measurement speed V = 0,1 mm/s) | Z <sub>0</sub>   | 18              | nm   | uzo             | 9     | nm      | Uniform   | 0,5774     | Czo               | 0,020634         |       |                  | 0,011   |                 | nm²             |                | 0,1072          | 100 |
| Uncertainty caused by inexact knowledge of<br>plastic deformation (for metallic standards)   | Z <sub>pl</sub>  | 0               | nm   | u <sub>pl</sub> | 0     | nm      | Uniform   | 0,5774     | C <sub>pl</sub>   | 1,00000          |       |                  | 0,0     |                 | nm²             |                | 0,0000          | 100 |
| Alignment error of the curve fitting (A)   | Ptr              | 10              | nm   | UPtr            | 2,5   | nm      | Uniform   | 0,5774     | CPtr              | 1,00000          |       |                  | 2       |                 | nm <sup>2</sup> | 1 [            | 1,4434          | 100 |
| Dm   | Dm               | 50244,6         | nm   | u <sub>Dm</sub> | 25    | nm      | Normal    | 0.5        | CDm               | 0,000012         |       |                  | 2,0E-08 |                 | nm <sup>2</sup> | 1 [            | 0,0001          | 100 |
| Linear thermal expansion coefficient of the<br>groove depth standard   | atest            | 16,6E-6         | 1/K  | u <sub>a</sub>  | 5E-07 | 1/K     | Uniform   | 0,5774     | Ca                | 35171,22         |       |                  | 0,0     |                 | nm <sup>2</sup> | 1              | 0,0102          | 100 |
| ∆T: (Test groove depth standard's temperature - 20) °C   | ΔΤ               | 0,7             | °C   | UΔT             | 0,3   | °C      | Normal    | 0,5        | C <sub>AT</sub>   | 0,834060         |       |                  | 0,0     |                 | nm <sup>2</sup> | ] [            | 0,1251          | 100 |
| Number of profile points at the top profile sections   | n <sub>h</sub>   | 4000            |      |                 |       |         |           |            |                   |                  |       |                  |         |                 |                 |                | Total           |     |
| Number of profile points at the bottom profile section   | n                | 5690            |      |                 |       |         |           |            |                   |                  |       |                  |         |                 |                 | Veff           | 123             |     |
|  |                  |                 |      |                 |       |         |           | TOTAL      | ARIANC            | E                |       | u <sup>2</sup> = | 102,1   | +               | 1,9E-07         | D <sup>2</sup> | nm <sup>2</sup> | ]   |
|  |                  |                 |      |                 |       |         |           | Standard   | Uncerta           | inty             |       | u =              | 24,1    |                 |                 |                | nm              |     |

#### Table 31 UME standard uncertainty budget for the groove depth 50 $\mu$ m

D<sub>n</sub> : Groove depth (Un: Uncertainty of Ref. groove depth standard)

- P<sub>tmy</sub> : Inaccuracy of measurement location on a groove of the Ref. groove depth standard. It is given as G\*a<sub>y</sub>. G = 20 nm/mm and a<sub>y</sub> = 0.05 mm. So G\*a<sub>y</sub> = 1 nm
- b : Reproducibility on the groove of the Ref. groove depth standard. 5 different measurement locations, 3 repetitions at each position ( $m_t = 15$ )
- $\alpha_r$  : Linear thermal expansion coefficient of the Ref. groove depth standard
- $\Delta T_r$  : (Ref. Groove depth standard's temperature 20) °C
- $D_m$  : Topography of test standard for 3 different measurement positions (m<sub>t</sub> = 9)

- z<sub>ref</sub> : Straightness deviation of the datum of the device (Wt measured on an optical flat)
- Background noise (Rzo measured on an optical flat without Is filter for Dx = 0.0001 mm, measurement speed V = 0.1 mm/s)
- z<sub>pl</sub> : Uncertainty caused by inexact knowledge of plastic deformation (for metallic standards)
- A : Alignment error of the curve fitting (Residual roughness Ptr)
- $\alpha_t$  : Linear thermal expansion coefficient of the test groove depth standard
- $\Delta T_t$  : (Test groove depth standard's temperature 20) °C
- n<sub>h</sub> : Number of profile points at the top profile sections
- $n_{l} \hfill :$  Number of profile points at the bottom profile section

#### 11.9 VNIIMS

 Table 32 VNIIMS standard uncertainty budget for all grooves

| quantity       | estimate       | uncertainty                    | probability  | sensitivity | uncertainty                                      | degrees of                              |
|----------------|----------------|--------------------------------|--------------|-------------|--|---|
| Xi             | <i>x</i> i, μm | <i>u</i> (x <sub>i</sub> ), μm | distribution | coefficient | contribution <i>u</i> <sub>i</sub> ( <i>d</i> ), | freedom                                 |
|                |                |                                |              | Ci          | μm   | Vi                                      |
| Uncertainty    |                |                                |              |             |  |   |
| of calibration | 0              | 0.003                          | N            | 1           | 0.0015   | ~                                       |
| standard       |                |                                |              |             |  |   |
| Self-noise     | 0              | 0.0042                         | R            | 1           | 0.00243  | 8                                       |
| Sensor         | 0              | 0.0032                         | R            | 1           | 0.00185  | ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~ |
| resolution     | 0              | 0.0032                         | K            | Ŧ           | 0.00185  |   |
| Sensor         | 0              |                                | N            | 1           |  | ~                                       |
| nonlinearity   | 0              | 0.007+0.003 H                  | IN           | Ŧ           | 0.0033-0.0013 H                                  | ~                                       |
| Datum bar      | 0              | 0.02                           | N            | 1           | 0.01   | ~                                       |
| Straightness   | U              | 0.02                           | IN           | L           | 0.01   | 3                                       |

#### 11.10 VTT

Table 33 VTT standard uncertainty budget for the three deeper grooves (900/600/200  $\mu$ m)

| Quantity<br><i>X</i> i                    | Estimate<br><i>x</i> i | Uncertainty<br>u(x <sub>i</sub> ) | Probability distribution | Sensitivity<br>coefficient | Uncertainty<br>contribution              | Degrees of<br>freedom |
|---|------------------------|-----------------------------------|--------------------------|----------------------------|--|-----------------------|
| periodic<br>nonlinearity                  | 0                      | 1.0 nm                            | R                        | 1                          | 1.0 nm                                   | 20                    |
| repeatability<br>σ <sub>r</sub>           | 0                      | 3.3 nm                            | N                        | 1                          | 3.3 nm                                   | 20                    |
| scale<br>nonlinearity<br>σ <sub>lin</sub> | 0                      | 144 × 10 <sup>-6</sup>            | R                        | 1                          | 144 × 10 <sup>-6</sup> ×<br><i>d</i>     | 100                   |
| amplification error $\sigma_s$            | 0                      | 10.6 × 10 <sup>-6</sup>           | N                        | d                          | $\frac{10.6 \times 10^{-6} \times d}{d}$ | 20                    |

| temperature<br>correction<br>factor T <sub>corr</sub> | <i>16.6</i> × 10⁻⁰/°C | 0.5 × 10⁻ੰ/°C | Ν                | 0.4°C × d                          | $0.2 \times 10^{-6} \times d$         | 100  |
|---|-----------------------|---------------|------------------|------------------------------------|---------------------------------------|------|
| temperature<br>T-20°C                                 | 0.4°C                 | 0.04°C        | Ν                | 16.6 × 10⁻ <sup>6</sup><br>/°C × d | 0.66 × 10 <sup>-6</sup> ×<br><i>d</i> | 100  |
| total<br>standard<br>uncertainty<br>u(d)              | (EN 1                 | 9_7)          | $\sqrt{(3.5nm)}$ | $^{2} + (144 \times$               | $10^{-6} \times d)^2$                 | ≥101 |

Table 34 VTT standard uncertainty budget for the three silicon grooves (50/20/5  $\mu m)$ 

| Quantity  | Estimat                     | Uncertainty             | Probabili   | Sensitivity                                     | Uncertainty                          | Degrees of |
|---|-----------------------------|-------------------------|---|---|--------------------------------------|------------|
| Xi  | е                           | u(x <sub>i</sub> )      | ty  | coefficient                                     | contribution                         | freedom    |
|   | Xi                          |                         | distributi  | Ci  | ui(d)                                | Vi         |
|   |                             |                         | on  |   |                                      |            |
| periodic nonlinearity                               | 0                           | 1.0 nm                  | R   | 1   | 1.0 nm                               | 20         |
| repeatability $\sigma_r$                            | 0                           | 3.3 nm                  | Ν   | 1   | 3.3 nm                               | 20         |
| scale nonlinearity $\sigma_{\text{lin}}$            | 0                           | 144 × 10 <sup>-6</sup>  | R   | 1   | 144 × 10 <sup>-6</sup> × <i>d</i>    | 100        |
| amplification error $\sigma_s$                      | 0                           | 10.6 × 10 <sup>-6</sup> | N   | d   | $10.6 \times 10^{-6} \times d$       | 20         |
| temperature<br>correction factor T <sub>corr</sub>  | 2.56 ×<br>10⁻⁶ /°C          | 0.5 × 10⁻⁶ /°C          | N   | 0.1°C × <i>d</i>                                | $50 \times 10^{-9} \times d$         | 100        |
| temperature<br>T-20°C                               | -0.1°C                      | 0.02 C                  | N   | 0.256 × 10 <sup>-</sup><br><sup>6</sup> /°C × d | 5.1 × 10 <sup>-9</sup> ×<br><i>d</i> | 100        |
| total standard<br>uncertainty <i>u</i> ( <i>d</i> ) | (SN 497, SN 499, SN<br>502) |                         | $\sqrt{(3.5 nm)^2 + (144 \times 10^{-6} \times d)^2}$ |   |                                      | ≥25        |

## 12 Appendix D Cleaning procedure for artefact EN19\_7 at BEV

The cleaning was performed iteratively under microscopic control.

1. Cleaning sample with purified compressed gas  $\rightarrow$  a few of the larger particles were removed only.

2. Soaking the sample in 2-Propanol overnight, drying with purified compressed gas  $\rightarrow$  no visible change.

3. Soaking the sample in acetone overnight, drying with purified compressed gas  $\rightarrow$  no visible change.

4. Ultrasonic bath for 3 minutes in 2-Propanol at 20 °C, drying with purified compressed gas  $\rightarrow$  no visible change but some of the finer particles were removed.

5. Ultrasonic bath for 3 minutes in acetone at 20 °C, drying with purified compressed gas  $\rightarrow$  no visible change.

6. Wiping the lands of sample with lens cleaning tissue soaked in acetone approximately 10 times. No force applied  $\rightarrow$  no visible change.

5. Wiping the lands and grooves with lens cleaning tissue soaked in acetone and Q-tips applying increasing force with the wooden handle  $\rightarrow$  the colored surface layer gradually disappears. After some

100 moves the appearance of grooves and lands become visually identical. The cleaning was stopped at this stage.

The stained surface layer was very difficult to remove and resemble corrosion products.

Used cleaning supplies:

- Cotton Tipped Applicators (Puritan, 15 cm, wood handle, Ref.: 806-WC)
- Lens Cleaning Tissue (ThorLabs, MC 50E)
- Airduster GDB (Electrolube, Ref.: GDP400)
- Acetone (residue analysis grade, UN1090, AppliChem)
- 2-Propanol (technical, VWR Chemicals)
- Ultrasonic Bath (EMAG, Emmi-40HC)

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