

STEERING UTC(k) TO UTC  
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1. Introduction
2. Prediction
3. Steering Options

# Omnipresence of Steering

TAI = EAL + frequency steers to primary frequency standards

(calibrated to meet definition of the second )

(EAL = ave of >200 clocks, including USNO's)

UTC = TAI + leap seconds

(crude steers, in phase, to Earth's rotation)

UTC(k) = TA(k) + steers to UTC = realization of UTC by laboratory k

(TA(k) = ave of Lab\_k's clocks)

GPS\* = Unsteered GPS clocks + steers to UTC(USNO) [in acceleration]

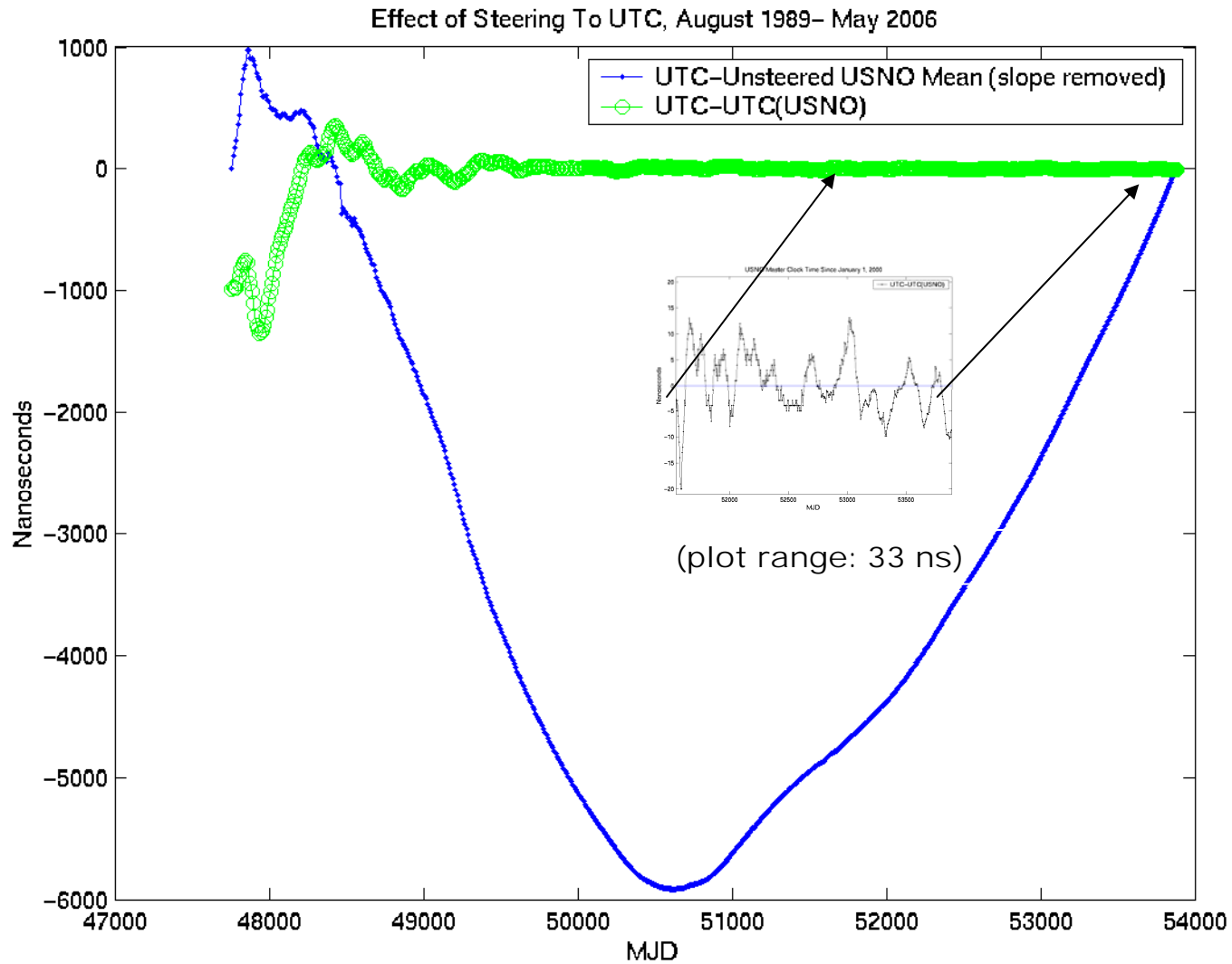
(Composite Clock= implicit average of steered satellite and monitor station clocks)

Cell Phone's Time = crystal + steers to UTC(k) or GPS\*

Atomic Clock's time = clock's crystal + steers to atomic frequencies

(GPS\* denotes GPS Time with leap seconds added)

# Improvement Due to Steering



# How Timing Labs Steer to UTC

- Some don't steer at all
- Others wait until UTC-UTC(k) is “too large”
  - Step rate of UTC(k)
  - Step phase of UTC(k)
- Better method:
  - First estimate future UTC-UTC(k)
  - Then steer UTC(k) so as to reduce UTC-UTC(k)
    - Do not jump your phase
    - Do adjust your frequency
      - Adjust Master Clock's voltage parameters
      - Or adjust microstepper/AOG/equivalent
      - Or software steer

# Rest of This Talk

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- Part II: State Estimation: model of UTC-UTC(k)
- Part III: Gains for Proportional Steering
  - $\text{Steer} = g_X * \text{Phase} + g_Y * \text{Freq} + g_Z * \text{Drift}$
  - Described by Gain Vector:  $(g_X, g_Y, g_Z)$
- Separation Principle: Optimal control (gain) is independent of optimal state estimation

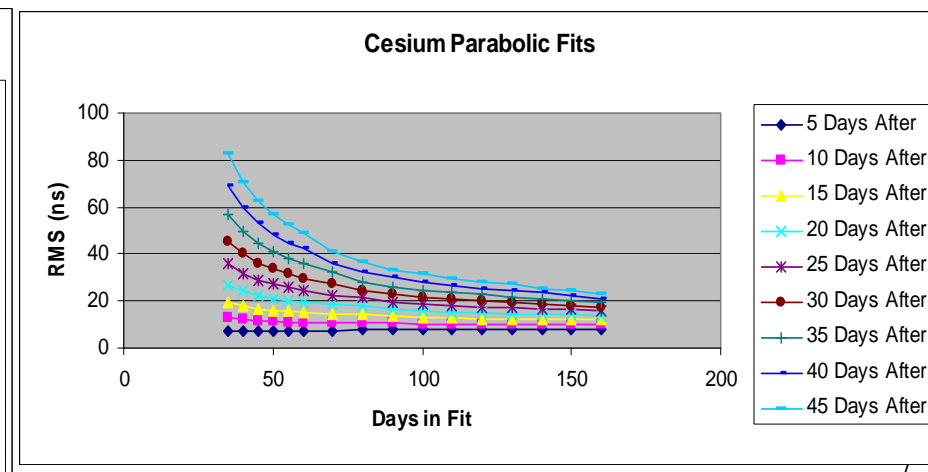
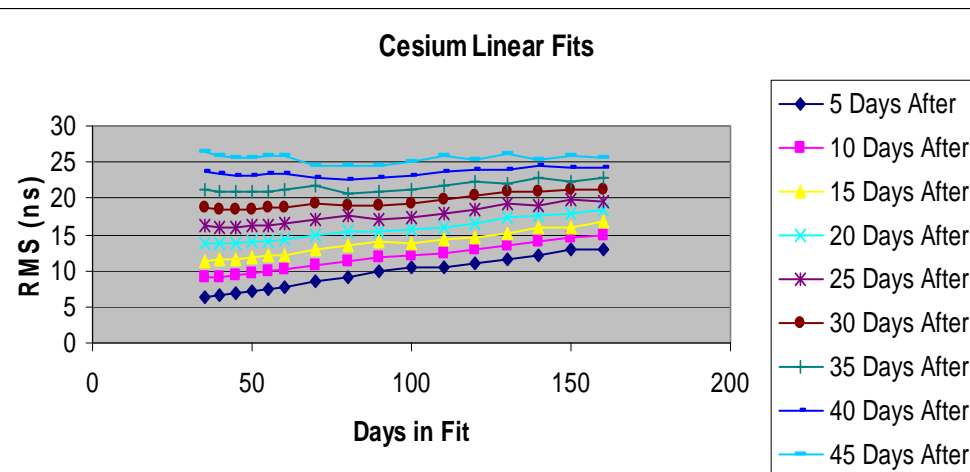
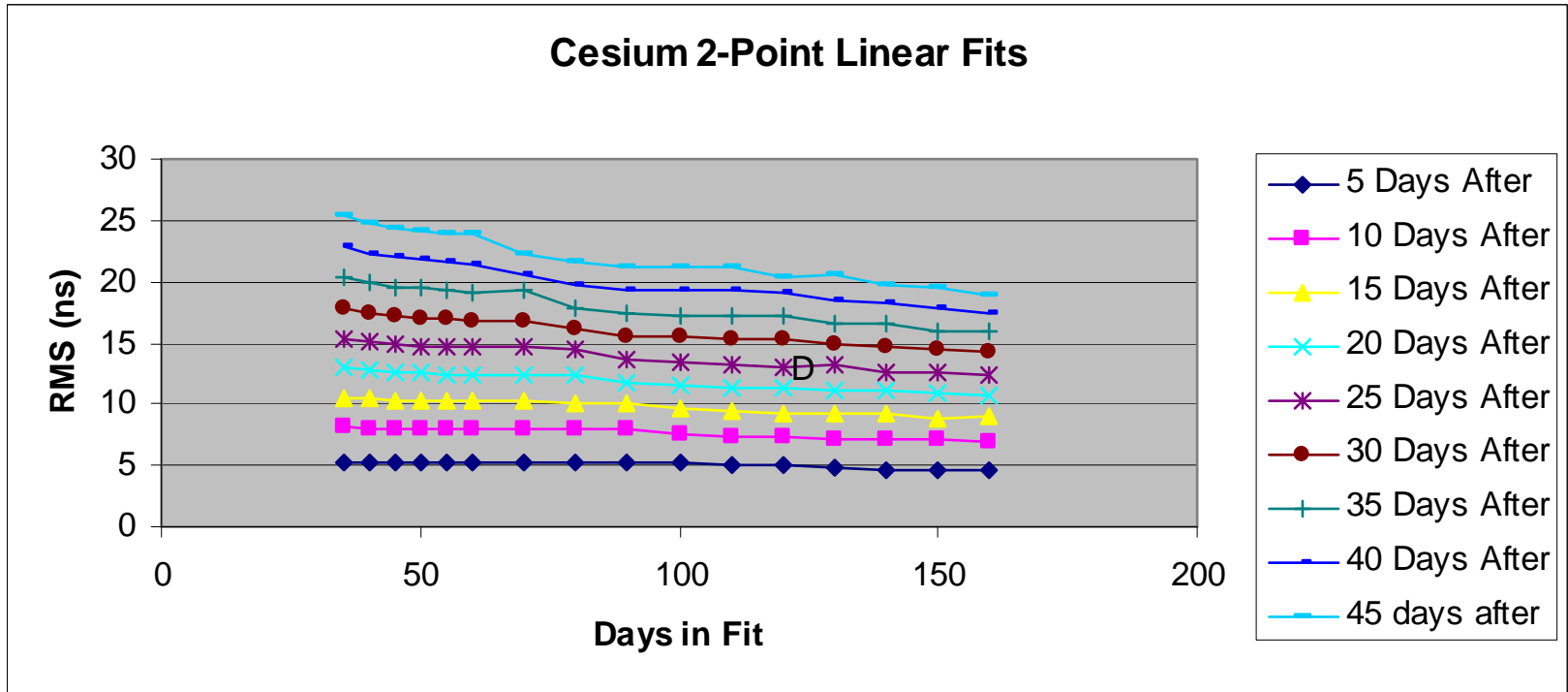
# Part II: Estimate UTC-UTC(k)

1. Start with published Circular T values of UTC-UTC(k)
2. Convert to EAL minus some unsteered real-time timescale
  - Timescale usually internal, could even be one cesium
  - Timescale could also be external real-time UTC realization
    - GPS makes UTC(USNO) easy to use, SIM makes UTC(NIST) easy too
3. Compute EAL-timescale
4. Extrapolate to future
5. Convert extrapolation to prediction of UTC-UTC(k)
  - Add back in the steers you took out in step 2
  - Future steers of EAL to generate UTC, from Circular T

# Extrapolating EAL-timescale

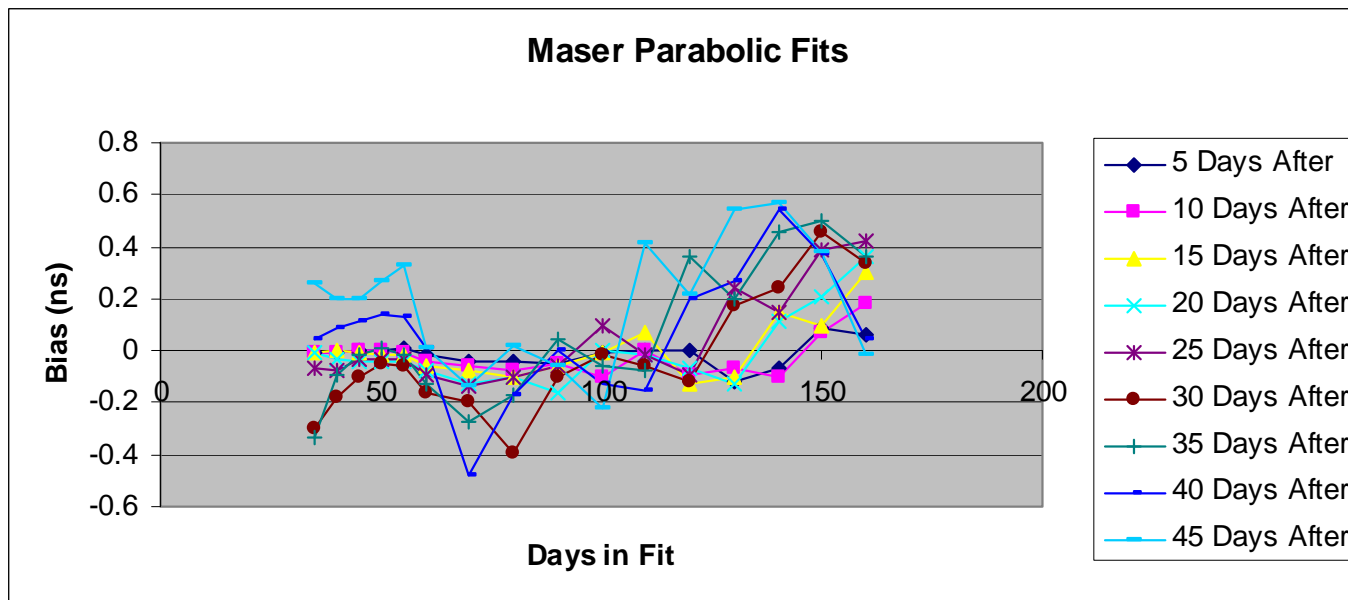
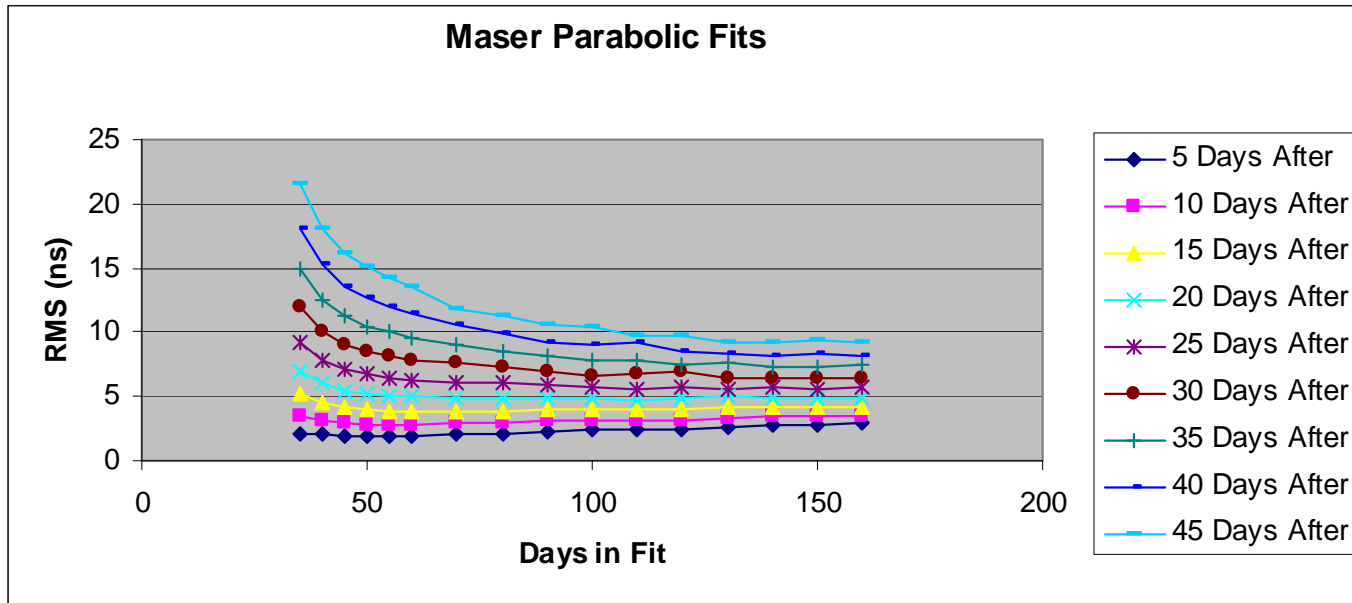
- Polynomial Fit
  - Fit Order: linear for Cesiums, quadratic for Masers
  - How far back in time to fit to? (recommend 60 days)
  - Fit in frequency domain, not phase
    - Because frequency noise is white
    - Simple method for cesiums:
      - Use only first and last phase points
      - Last point minus first point yields average frequency
- Other ways exist
  - Auto-Regressive Integrated Moving Average (ARIMA) and State Space Models
  - Kalman Filters are one form of estimator

# Extrapolating EAL-cesiums



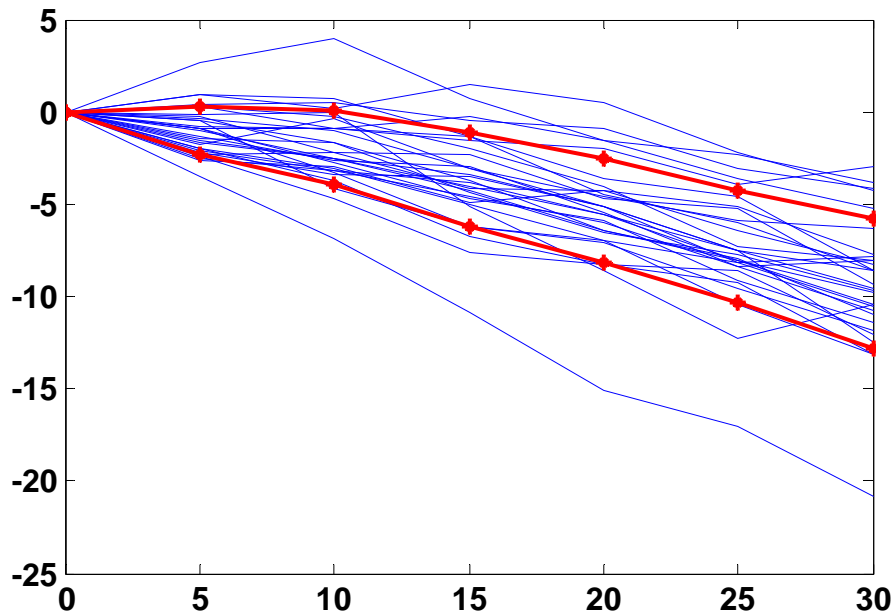


# Extrapolating EAL-USNO masers

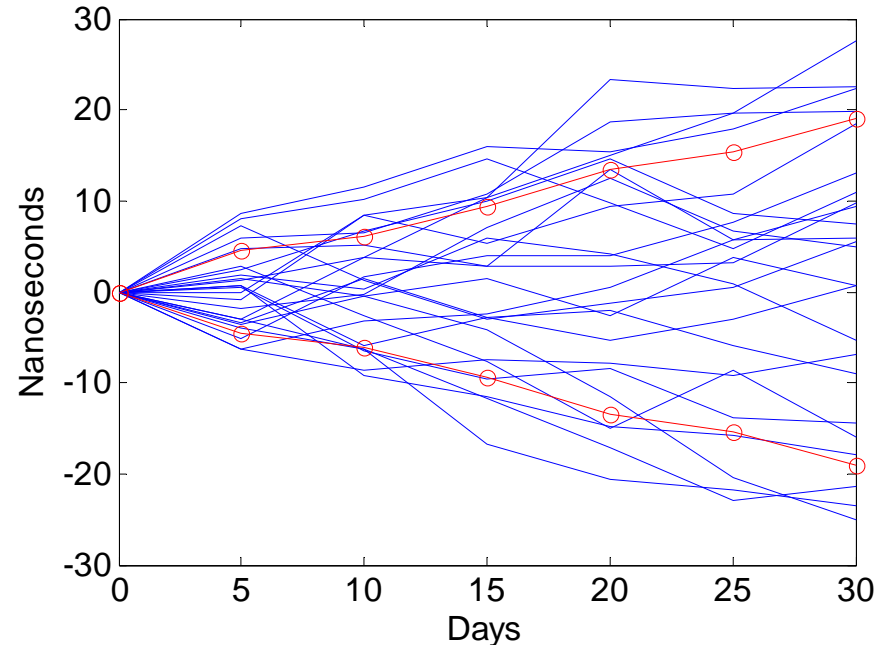


# Masers and Cesiums as EAL Predictors

3-year test period (2006-2008)



Maser deviations after fit period



Cesium deviations after fit period

Viewgraph and Analysis from Panfilo and Arias, EFTF-09  
See also: Matsakis et al., ION Annual Meeting, June 2000

# Part III: Setting the Gain Vector

- $\text{Steer} = g_X * \text{Phase} + g_Y * \text{Freq} + g_Z * \text{Drift}$
- ALL steering involves a trade-off between:
  - frequency offset
  - time offset
  - control effort
    - Control perturbs local clock
- Linear Quadratic Gaussian (LQG) theory can compute the optimal gains for your goals.

See Koppang and Leland, 1999, IEEE Trans.  
Ultrason. Ferroelect., Freq. Control 46, pp 517-522.

See also Appendix IV.

# Some Ways to Set Gains

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- LQG Theory
  - A compromise between goals
- Pole Placement
  - Set response times
- Gentle Steering
  - Minimum amount of steering to achieve desired phase and frequency shift

# *MILD* Recommendation

- Estimate difference in UTC-UTC(k), 30 days into the future
  - When next Circular T comes
  - Assuming you did nothing
- Steer so that 30 days into the future you will have removed 50% of the predicted frequency difference and 50% of the phase difference
  - Ignore frequency drift for steering
- Make one steer every 6 days
  - Use formula on next slide (N=5) ...

# "Gentle Steering"

Change clock's time by  $\Delta x$  and frequency by  $\Delta y$

Use  $N$  steers of magnitude  $U_n$  spaced  $\tau$  seconds apart

Minimum Amount of Control Effort ( $U$ )

Ideal for steering to Circular T

<http://www.pttimeeting.org>: Koppang and Matsakis, PTTI-00, pp. 277-284

$$U = -\frac{6}{N(N+1)} \begin{bmatrix} \frac{1}{\tau} & \frac{2N-1}{3} \\ \frac{1}{\tau} \left(1 - \frac{2}{N-1}\right) & -1 + \frac{2N-1}{3} \\ \vdots & \vdots \\ -\frac{1}{\tau} & -(N-1) + \frac{2N-1}{3} \end{bmatrix} \begin{bmatrix} \Delta x \\ \Delta y \end{bmatrix}$$

# Warning !

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- Be careful what you ask for ...
- With control theory, you might get it.
- Therefore, simulate control performance